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Black hole jets on the scale of the Cosmic Web

Summary Paragraph

When sustained for megayears [1, 2], high-power jets from supermassive black holes become the Uni-23 verse's largest galaxy-made structures [3]. By pumping electrons, atomic nuclei, and magnetic fields 24 25 into the intergalactic medium, these energetic flows affect the distribution of matter and magnetism in the Cosmic Web [4-6], and could have a sweeping cosmological influence if they reached far at 26 early epochs. For the last fifty years, the known size range of black hole jet pairs terminated at 4.6-27 5.0 Mpc [7–9], or 20–30% of a cosmic void radius in the Local Universe [10]. An observational 28 lack of longer jets, as well as theoretical results [11], thus suggested a growth limit at $\sim 5 \text{ Mpc}$ [12]. Here we report observations of a radio structure spanning ~ 7 Mpc, or $\sim 66\%$ of a coeval cosmic 30 void radius, apparently generated by a black hole between $4.4^{+0.2}_{-0.7}$ -6.3 Gyr after the Big Bang. The 31 structure consists of a northern lobe, a northern jet, a core, a southern jet with an inner hotspot, 32 and a southern outer hotspot with a backflow. This system demonstrates that jets can avoid destruc-33 tion by magnetohydrodynamical instabilities over cosmological distances, even at epochs when the 34 Universe was $7-15^{+6}_{-2}$ times denser than it is today. How jets can retain such long-lived coherence is 35 presently unknown. 36

37 Keywords: Active galactic nuclei, astrophysical jets, giant radio galaxies, intergalactic medium

³⁸ 1 Main text

22

To quantify the impact of black hole energy transport on the intergalactic medium (IGM), radio images from the International LOFAR Telescope (ILT) have recently been searched [e.g. 9, 13–15] for Mpcscale galactic outflows. In particular, our team systematically scanned the ILT's ongoing northern sky

- 42 survey at wavelength $\lambda = 2.08$ m both with machine learning and by eye the latter with significant
- ⁴³ contributions from citizen scientists [16]. This endeavour has increased the number of known Mpc-scale
- outflows from a few hundred to over eleven thousand [15]. Our largest find is the outflow shown in Fig. 1, which we name Porphyrion. The source, of angular length $\phi = 13.4' \pm 0.1'$, appears unusually thin.



Fig. 1: Deep radio images of a 7 Mpc-long, black hole-driven outflow at central wavelengths $\lambda = 2.08$ m and $\lambda = 0.46$ m. These images, (a) and (b), were taken with the ILT and uGMRT, respectively, and have resolutions of 6.2" and 4.3". Panel (a)'s inset shows ILT VLBI imagery at $\lambda = 2.08$ m and a resolution of 0.4". Panel (b)'s inset shows Legacy DR10 optical-infrared imagery. The larger images cover $15' \times 15'$ of sky, whilst the insets cover $1' \times 1'$. For scale, we show the stellar Milky Way disk (diameter: 50 kpc) and a ten times inflated version.



Fig. 2: In our imagery, only the southern host galaxy candidate features a radio extension along Porphyrion's overarching jet axis. For the central $3' \times 3'$ sky area, we show a uGMRT image at $\lambda = 0.46$ m and 3.6'' resolution. We detect the southern galaxy's radio extension, directed towards the north-northeast, at 5 s.d. (σ) significance. The contours denote 3σ , 5σ , 10σ , and 100σ .

To investigate from which galaxy along the jet axis the outflow originates, we processed ILT very-long-45 baseline interferometry (VLBI) data of the central $4' \times 4'$. At a spatial resolution of 3 kpc, the image 46 (Fig. 1's top panel inset and Fig. 2.2) shows lone, unresolved radio sources in two galaxies, in both 47 cases implying active accretion onto a supermassive black hole (SMBH). Because the detection of jets 48 near either black hole (and along the overarching NNE–SSW axis) would clarify Porphyrion's origin, we 49 performed deep follow-up observations with the Upgraded Giant Metrewave Radio Telescope (uGMRT) at $\lambda = 0.46$ m. The resulting image and ancillary DESI Legacy Imaging Surveys (Legacy) optical-infrared data (Fig. 1's bottom panel) reveal that the outflow protrudes from a massive $(M_{\star} = 6.7^{+1.4}_{-1.4} \cdot 10^{11} M_{\odot})$ galaxy. This is visually clear in Fig. 2, which is processed to highlight the radio morphologies of the two central galaxies. Of these, the southernmost galaxy uniquely displays a 5σ extension along Porphyrion's 54 overarching jet axis. We observed this galaxy with the Low Resolution Imaging Spectrometer (LRIS) on the W. M. Keck Observatory's Keck I Telescope, measuring a spectroscopic redshift $z = 0.896 \pm 0.001$ (Fig. 3's top panel). We witness Porphyrion at $t_{BB} = 6.3$ Gyr after the Big Bang. 57

The outflow's angular length and redshift entail a sky-projected length $l_{\rm p} = 6.43 \pm 0.05$ Mpc. This 58 makes Porphyrion the projectively longest known structure generated by an astrophysical body. The 59 outflow's total length exceeds this projected length, but by how much depends on the unknown inclination 60 of the jets with respect to the sky plane. Deprojection formulae [14] predict a total length $l = 6.8^{+1.2}_{-0.3}$ Mpc, 61 with expectation $\mathbb{E}[L \mid L_p = l_p] = 7.28 \pm 0.05$ Mpc (Methods). We thus estimate Porphyrion to be \sim 7 Mpc long in total. Spanning \sim 66% of the radius of a typical cosmic void at its redshift, the outflow is truly cosmological. Surprisingly, SMBH jets can remain collimated over several megaparsecs, despite 64 the growth of (magneto)hydrodynamical (MHD) instabilities — chiefly Kelvin–Helmholtz instabilities 65 predicted theoretically and seen in simulations of shorter jets [e.g. 11]. Similarly, prolonged entrainment 66 of mass from the IGM, even at $z \gtrsim 1$, does not necessarily destabilise jets. No MHD simulations of Mpc-67 scale jets yet exist: the spatio-temporal grids required imply a numerical cost $\sim 10^2$ times higher than 68 that of state-of-the-art runs. Outflows like Porphyrion thus offer a window into a jet physics regime that, 69 at present, cannot be explored numerically.

Active galactic nuclei (AGN) with accretion disks extending to the innermost stable circular orbits of their SMBHs efficiently convert the gravitational potential energy of infalling matter into radiation, and are thus called radiatively efficient (RE); all others are called radiatively inefficient (RI) [17, 18].



Fig. 3: Both rest-frame ultraviolet-optical spectroscopy and radio-ultraviolet photometry demonstrate that the outflow's host galaxy harbours an RE AGN. a) LRIS spectrum exhibiting hydrogen, carbon, oxygen, and neon emission. The forbidden lines from multiply ionised oxygen and neon (dark red) could not be generated by even the hottest stars, and instead stem from the narrow-line region of an RE AGN at a redshift $z = 0.896 \pm 0.001$. b) Bayesian inference of the galaxy's SED (Methods) favours the presence of an AGN accretion disk (dark blue) with an obscuring torus (purple), again indicating radiative efficiency.

⁷⁴ In RE AGN, the luminous accretion disk photo-ionises a circumnuclear region emitting narrow, and ⁷⁵ often forbidden, spectral lines. The Keck-observed prominence of forbidden ultraviolet-optical lines from ⁷⁶ oxygen and neon (chiefly that of the [O III] λ 5007 line, which is 10.3 ± 0.2 times brighter than the H β ⁷⁷ line) therefore reveals the presence of an RE AGN [19]. Bayesian inference of the galaxy's spectral ⁷⁸ energy distribution (SED; Methods and Fig. 3's bottom panel) independently suggests the presence of a ⁷⁹ luminous SMBH accretion disk with an obscuring torus: our model requires these structures to explain ⁸⁰ the observed infrared (WISE) and near-ultraviolet (Legacy) flux levels, which exceed those possible with ⁸¹ cold dust and stars alone. ⁸² By contrast, all previous record-length outflows, such as 3C 236 ($l_{\rm p} = 4.6$ Mpc; [7]), J1420-0545 ($l_{\rm p} =$

⁸² By contrast, all previous record-length outflows, such as 3C 236 ($l_p = 4.6 \text{ Mpc}; [7]$), J1420–0545 ($l_p = 4.9 \text{ Mpc}; [8]$), and Alcyoneus ($l_p = 5.0 \text{ Mpc}; [9]$), are fuelled by RI AGN in recent history ($t_{BB} = 10.2-12.4 \text{ Gyr}$). Whereas RI AGN occur primarily in evolved, 'red and dead' ellipticals [17], RE AGN feature vigorous gas inflows and are thus generally found in star-forming galaxies. Indeed, in the first billions of years of cosmic time, RE AGN dominated the radio-luminous AGN population [20]. The potential of Mpc-scale outflows to spread cosmic rays, heat, heavy atoms, and magnetic fields through the IGM is particularly high if large specimina could emerge from the type of AGN abundant at early epochs,



Fig. 4: By superimposing Porphyrion's total length and radio luminosity on evolutionary tracks from dynamical modelling, we inferred the outflow's two-sided jet power and age. We assumed the host galaxy to reside in a galaxy group bordering voids, through which the jets eventually travel. The width and height of Porphyrion's uncertainty ellipse both cover 68% of probability centred around the median (green dot).

when the Universe was smaller. The discovery of a 7 Mpc-long, RE AGN-fuelled outflow before cosmic
 half-time therefore highlights the hitherto understudied cosmological transport capabilities of Mpc-scale
 outflows.

In the Local Universe, $\sim 30\%$ of all luminous Mpc-scale outflows reside in galaxy clusters, $\sim 60\%$ in 92 galaxy groups, and the remaining $\sim 10\%$ in more dilute parts of filaments, in sheets, or in voids [21]. The Legacy DR10 (shown in Fig. 1's bottom panel inset) suggests that Porphyrion does not originate from a 94 galaxy cluster: the closest known cluster [22] lies at a comoving distance of 30^{+12}_{-17} Mpc, or 31^{+14}_{-16} cluster radii (Methods). The nearest Planck Sunyaev–Zel'dovich detection [23] is ~2° away. Concordantly, studies 96 have found that jet-fuelling RE AGN avoid rich environments [24, 25]. In a sphere with a comoving 97 radius of 10 Mpc centred around Porphyrion's host, we counted 35 ± 6 other Legacy-detected galaxies. 98 By also performing galactic neighbour counts for a control sample of galaxies at comparable redshifts, 99 and by assuming that galactic neighbour counts increase with circumgalactic Cosmic Web density, we estimated Porphyrion's circumgalactic Cosmic Web density percentile to be 42^{+26}_{-23} % (Methods). This suggests that Porphyrion does not originate from a void. The straightness of the outflow implies a low peculiar speed ($v_{\rm p} \lesssim 10^2 \text{ km s}^{-1}$), consistent with the host being at the bottom of a local gravitational potential well. The evidence implies that Porphyrion originates from a Cosmic Web filament, and from 104 a galaxy group in particular. Vast voids, which make up the bulk ($\sim 80\%$) of the Universe's volume [26], surround such structures in most directions. Jets as long as Porphyrion's thus encounter voidlike densities and temperatures with considerable probability. Indeed, the collimated nature of the jets favours scenarios in which they descend into voids, as jets gain resilience against Kelvin-Helmholtz 108 instabilities when the ambient density declines [e.g. 11]. Dynamical modelling suggests a two-sided jet power $Q = 1.3 \pm 0.1 \cdot 10^{39}$ W and an age $T = 1.9^{+0.7}_{-0.2}$ Gyr (Fig. 4; Methods). The outflow's average expansion speed v = 0.012 c, comparable to Alcyoneus' [9]. In voids and the warm-hot IGM, the speed 111 of sound $c_{\rm s} \sim 10^0 - 10^1$ km s⁻¹: the jets grow hypersonically at Mach numbers $\mathcal{M} \sim 10^2 - 10^3$ and drive 112 strong shocks into voids. Porphyrion's jets have carried an energy $E = QT = 8^{+2}_{-1} \cdot 10^{55}$ J into the IGM 113 — an amount comparable to the energy released during galaxy cluster mergers [e.g. 27]. This suggests 114 that the outflow is among the most energetic post-Big Bang events to have occurred in its Cosmic Web region. Even though the SMBH might have gained a significant fraction of its mass while powering the jets ($\Delta M_{\bullet} > 2\frac{E}{c^2} = 9^{+2}_{-1} \cdot 10^8 M_{\odot}$), it appears to have maintained a constant spin axis throughout 117 gigayears of activity. Shocks running perpendicular to the jets dissipate enough heat into the filament 118 to increase its temperature by $\Delta T \sim 10^7$ K and its radius by $\Delta r \sim 1$ Mpc (Methods). Outflows like 119 Porphyrion thus locally alter the Cosmic Web's shape. 120

Figure 4 illustrates that the radio luminosities of Mpc-long outflows with constant jet power initially decrease before stabilising to a jet power-dependent level. Active outflows not only lengthen, but also grow volumetrically [15]; consequently, the mean radio luminosity per unit of lobal volume drops over time. In turn, lobal radio surface brightnesses decrease [21], impeding outflow detection [14, 15]. As 124 Fig. 1 evinces, Porphyrion borders on the noise of leading current-day telescopes; thus, outflows further progressed on the same evolutionary track hitherto evade detection. Similar outflows are likewise undetectable at lower jet powers and at higher redshifts, where increased inverse Compton scattering with the CMB diverts electron energy away from synchrotron radiation — causing lower radio luminosities at 128 fixed jet powers [28]. Problematically, cosmological surface brightness dimming further reduces radio sur-129 face brightnesses by a factor of $(1+z)^{3-\alpha}$, where α is the radio spectral index. Statistical modelling [14, 130 15] indeed suggests that the detectable population is just the tip of the iceberg: owing to their apparent faintness, most Mpc-scale outflows are still concealed by noise. These arguments, and the fact that our search covered only $\sim 15\%$ of the sky, imply the existence of a hidden population of outflows with sizes 133 comparable to, and possibly larger than, Porphyrion's. 134

Porphyrion indicates that RE AGN may be at least as effective at generating Mpc-scale outflows as RI AGN are in the Local Universe. If the comoving number density of actively powered Mpc-scale 136 outflows has remained roughly constant over time at $\sim 10^1 (100 \text{ Mpc})^{-3} [14, 15]$, and a comoving vol-137 ume of $(100 \text{ Mpc})^3$ contains $\sim 10^2$ filaments, then there would exist $\sim 10^{-1}$ actively powered Mpc-scale 138 outflows in every filament at every instant. As their jets endure for $\sim 10^{-2}$ -10⁰ Gyr [1, 3, 9], $\sim 10^{1}$ 139 Mpc-scale outflows may have been generated in every filament throughout cosmic history. If jet pow-140 ers $Q \sim 10^{38}$ W are typical [1, 9, 28], Mpc-scale outflows induce significant heating ($\Delta T \sim 10^6$ K) 141 and expansion ($\Delta r \sim 10^{-1}$ Mpc) of cosmic filaments (Methods), which comprise the Universe's primary 142 baryon reservoir. Whereas AGN feedback has been known to maintain the thermodynamic state in the 143 $\sim 1 \text{ Mpc}^3$ -scale volumes of galaxy clusters, Porphyrion's discovery highlights the importance of black 144

¹⁴⁵ hole energy transport in the Cosmic Web at large.

146 **References**

- 1. Hardcastle, M. J. *et al.* Radio-loud AGN in the first LoTSS data release. The lifetimes and environmental impact of jet-driven sources. A&A **622**, A12 (2019).
- Perucho, M., Martí, J.-M. & Quilis, V. Long-term FRII jet evolution: clues from three-dimensional simulations. MNRAS
 482, 3718-3735 (2019).
- Dabhade, P., Saikia, D. J. & Mahato, M. Decoding the giant extragalactic radio sources. Journal of Astrophysics and Astronomy 44, 13 (2023).
- Ayromlou, M., Nelson, D. & Pillepich, A. Feedback reshapes the baryon distribution within haloes, in halo outskirts, and beyond: the closure radius from dwarfs to massive clusters. MNRAS 524, 5391-5410 (2023).
 Beck, A. M., Hanasz, M., Lesch, H., Remus, R. .-. & Stasyszyn, F. A. On the magnetic fields in voids. MNRAS 429, L60-L64
- (2013).
 Kazza, F. et al. Simulations of extragalactic magnetic fields and of their observables. Classical and Quantum Gravity 34, 234001 (2017).
- 159 7. Willis, A. G., Strom, R. G. & Wilson, A. S. 3C236, DA240; the largest radio sources known. Nature 250, 625–630 (1974).
- Machalski, J., Kozieł-Wierzbowska, D., Jamrozy, M. & Saikia, D. J. J1420-0545: The Radio Galaxy Larger than 3C 236. ApJ
 679, 149–155 (2008).
- 162 9. Oei, M. S. S. L. et al. The discovery of a radio galaxy of at least 5 Mpc. A&A 660, A2 (2022).
- 10. Correa, C. M. *et al.* Redshift-space effects in voids and their impact on cosmological tests. Part I: the void size function.
 MNRAS 500, 911–925 (2021).
- 11. Perucho, M. Dissipative Processes and Their Role in the Evolution of Radio Galaxies. Galaxies 7, 70 (2019).
- Andernach, H., Jiménez-Andrade, E. F. & Willis, A. G. Discovery of 178 Giant Radio Galaxies in 1059 deg² of the Rapid ASKAP Continuum Survey at 888 MHz. *Galaxies* 9, 99 (2021).
 Dabhade, P. *et al.* Giant radio galaxies in the LOFAR Two-metre Sky Survey. I. Radio and environmental properties. A&A
- 13. Dabhade, P. et al. Giant radio galaxies in the LOFAR Two-metre Sky Survey. I. Radio and environmental properties. A&A 635, A5 (2020).
 14. Oei, M. S. S. L. et al. Measuring the giant radio galaxy length distribution with the LoTSS. A&A 672, A163 (2023).
- Oei, M. S. S. L. et al. Measuring the giant radio galaxy length distribution with the LoTSS. A&A 672, A163 (2023).
 Mostert, R. I. J. et al. Constraining the giant radio galaxy population with machine learning and Bayesian inference. arXiv e-prints, arXiv:2405.00232 (2024).
- Hardcastle, M. J. *et al.* The LOFAR Two-Metre Sky Survey. VI. Optical identifications for the second data release. A&A
 678, A151 (2023).
- 175 17. Heckman, T. M. & Best, P. N. The Coevolution of Galaxies and Supermassive Black Holes: Insights from Surveys of the Contemporary Universe. ARA&A 52, 589–660 (2014).
- Hardcastle, M. Interpreting radiative efficiency in radio-loud AGNs. Nature Astronomy 2, 273-274 (2018).
 Buttiglione, S. et al. An optical spectroscopic survey of the 3CR sample of radio galaxies with z < 0.3. II. Spectroscopic
- 179 classes and accretion modes in radio-loud AGN. A&A 509, A6 (2010).
 20. Williams, W. L. *et al.* LOFAR-Boötes: properties of high- and low-excitation radio galaxies at 0.5 < z < 2.0. MNRAS 475,
- Winnams, W. L. et al. DOTATEBOOLES. Properties of high- and low-excitation radio galaxies at 0.5 < 2 < 2.0. Writers 419, 3429–3452 (2018).
 Oei, M. S. S. L. et al. Luminous giants populate the dense Cosmic Web: The radio luminosity-environmental density relation
- Cer, M. S. D. *et al.* Luminous grants populate the dense cosmic web. The radio funnosity-environmental density relation for radio galaxies in action. *arXiv e-prints*, arXiv:2404.17776 (2024).
 Wen, Z. L. & Han, J. L. A catalog of 1.58 million clusters of galaxies identified from the DESI Legacy Imaging Surveys.
- 22. Wen, Z. L. & Han, J. L. A catalog of 1.58 million clusters of galaxies identified from the DE51 Legacy imaging Surveys. arXiv e-prints, arXiv:2404.02002 (2024).
 23. Planck Collaboration et al. Planck 2015 results. XXVII. The second Planck catalogue of Sunyaev-Zeldovich sources. A&A
- Planck Collaboration *et al.* Planck 2015 results. XXVII. The second Planck catalogue of Sunyaev-Zeldovich sources. A&A
 594, A27 (2016).
 Ineson, J. *et al.* Radio-loud Active Galactic Nucleus: Is There a Link between Luminosity and Cluster Environment? ApJ
- Ineson, J. *et al.* Radio-loud Active Galactic Nucleus: Is There a Link between Luminosity and Cluster Environment? ApJ 770, 136 (2013).
- Ineson, J. et al. The link between accretion mode and environment in radio-loud active galaxies. MNRAS 453, 2682–2706 (2015).

26.192

193

Forero-Romero, J. E., Hoffman, Y., Gottlöber, S., Klypin, A. & Yepes, G. A dynamical classification of the cosmic web. MNRAS 396, 1815–1824 (2009).
van Weeren, R. J. et al. Radio observations of ZwCl 2341.1+0000: a double radio relic cluster. A&A 506, 1083–1094 (2009).
Hardcastle, M. J. A simulation-based analytic model of radio galaxies. MNRAS 475, 2768–2786 (2018). 27.194

195 28.

List of Figures 196

197	1	Deep radio images of a 7 Mpc–long, black hole–driven outflow at central wave-	
198		lengths $\lambda = 2.08$ m and $\lambda = 0.46$ m. These images, (a) and (b), were taken with the ILT	
199		and uGMRT, respectively, and have resolutions of $6.2''$ and $4.3''$. Panel (a)'s inset shows	
200		ILT VLBI imagery at $\lambda = 2.08$ m and a resolution of 0.4". Panel (b)'s inset shows Legacy	
201		DR10 optical–infrared imagery. The larger images cover $15' \times 15'$ of sky, whilst the insets	
202		cover $1' \times 1'$. For scale, we show the stellar Milky Way disk (diameter: 50 kpc) and a ten	
203		times inflated version.	2
204	2	In our imagery, only the southern host galaxy candidate features a radio exten-	
205		sion along Porphyrion's overarching jet axis. For the central $3' \times 3'$ sky area, we show	
206		a uGMRT image at $\lambda = 0.46$ m and $3.6''$ resolution. We detect the southern galaxy's radio	
207		extension, directed towards the north-northeast, at 5 s.d. (σ) significance. The contours	
208		denote 3σ , 5σ , 10σ , and 100σ .	3
209	3	Both rest-frame ultraviolet–optical spectroscopy and radio–ultraviolet pho-	
210		tometry demonstrate that the outflow's host galaxy harbours an RE AGN. a)	
211		LRIS spectrum exhibiting hydrogen, carbon, oxygen, and neon emission. The forbidden	
212		lines from multiply ionised oxygen and neon (dark red) could not be generated by even	
213		the hottest stars, and instead stem from the narrow-line region of an RE AGN at a red-	
214		shift $z = 0.896 \pm 0.001$. b) Bayesian inference of the galaxy's SED (Methods) favours the	
215		presence of an AGN accretion disk (dark blue) with an obscuring torus (purple), again	
216		indicating radiative efficiency.	4
217	4	By superimposing Porphyrion's total length and radio luminosity on evolu-	
218		tionary tracks from dynamical modelling, we inferred the outflow's two-sided	
219		jet power and age. We assumed the host galaxy to reside in a galaxy group border-	
220		ing voids, through which the jets eventually travel. The width and height of Porphyrion's	
221		uncertainty ellipse both cover 68% of probability centred around the median (green dot).	5

$_{222}$ 2 Methods

Throughout this work, we assume a flat, inflationary Λ CDM cosmological model with parameters from Planck Collaboration *et al.* [1]: h = 0.6766, $\Omega_{BM,0} = 0.0490$, $\Omega_{M,0} = 0.3111$, and $\Omega_{\Lambda,0} = 0.6889$. We define $\Omega_{DM,0} \coloneqq \Omega_{M,0} - \Omega_{BM,0} = 0.2621$ and $H_0 \coloneqq h \cdot 100$ km s⁻¹ Mpc⁻¹. Furthermore, we define the spectral index α so that it relates to flux density F_{ν} at frequency ν as $F_{\nu} \propto \nu^{\alpha}$. Under this convention, synchrotron spectral indices are *positive* (i.e. $\alpha = \frac{5}{2}$) for the lowest frequencies and *negative* for higher frequencies. As the restoring PSFs may not be perfectly circular, all reported resolutions are effective resolutions. In other works, Mpc-scale outflows are usually called 'giant radio galaxies'.¹

230 ILT observations and data reduction

The International LOFAR Telescope [ILT; 3] is exquisitely sensitive to the metre-wavelength synchrotron radiation generated by electrons and positrons in the first tens to hundreds of megayears after their acceleration to relativistic energies. Consequently, the second data release [DR2; 4] of the LOFAR Twometre Sky Survey [LoTSS; 5], the ILT's ongoing northern sky survey in the 120–168 MHz frequency band, has revealed millions of galaxies boasting supermassive black hole (SMBH) jets.

After discovering Porphyrion², the outflow presented in this work, we extracted a total of 16 hours of DDFacet-calibrated visibilities [6] from LoTSS pointings P228+60 and P233+60 (Project ID: LT5_007). Following van Weeren et al. [7], we subtracted all sources far away from the target, performed phase 238 shifting and averaging, and self-calibrated the resulting data. This removed residual ionospheric artefacts around ILTJ153004.28+602423.2, the brightest source in the arcminute-scale vicinity of the northern 240 lobe. We subsequently performed joint deconvolution on the recalibrated target visibilities with WSClean [8] using Briggs weighting -0.5, yielding the 6.2''-resolution image of Fig. 1's top panel. The noise level is 242 $\sigma = 25$ Jy deg⁻² at its lowest. The outflow appears thin: its width is nowhere more than a few percent of 243 its length. We defined Porphyrion's angular length as the largest possible great-circle distance between a 244 point in the southern hotspot and a point in the northern lobe. The arc connecting these points defines the overarching jet axis, and we measured its position angle to be $27 \pm 1^{\circ}$.

To investigate the presence of diffuse structure, we applied Gaussian tapering to the weights of the 247 recalibrated target visibilities. The taper's FWHM in the (u, v)-plane was chosen such that the FWHM of 248 the corresponding Gaussian in the sky plane equals 15". Again performing deconvolution with WSClean using Briggs weighting -0.5 (albeit in multi-scale mode this time), we obtained the 19.8"-resolution 250 image of Fig. 2.1. This image reveals the northern lobe more clearly. The noise level is $\sigma = 4.8$ Jy deg⁻². 251 To obtain a high-resolution image of Porphyrion, we reprocessed the P233+60 data, including 252 LOFAR's international stations, from scratch using the LOFAR-VLBI pipeline [9]. This pipeline builds upon the calibration pipeline for the Dutch part of the array to calibrate the international stations. We 254 derived the dispersive phase corrections and gain corrections for the international stations by calibrating against a bright and compact radio source near the target. In this case, we used the aforementioned ILTJ153004.28+602423.2, a known source from the Long-Baseline Calibrator Survey [LBCS; 10, 11]. To 257 reduce interference from unrelated radio sources in Porphyrion's angular vicinity, we phased up LOFAR's 258 core stations to narrow down the field of view and only considered data from long baselines to calculate the calibration solutions. With the calibration solutions applied in the direction of the target, we 260 again performed deconvolution with WSClean (but using Briggs weighting 0) to obtain a 0.4"-resolution 263 image, which we show partially in Fig. 1's top panel inset and fully in Fig. 2.2. The noise level is 262 $\sigma = 2.7 \cdot 10^3$ Jy deg⁻² at its lowest. This image, which covers the central one-third of the total jet system, 263 reveals synchrotron emission at 42σ significance from active galactic nuclei (AGN) in only two galax-264 ies, 19" apart. Both lie along the outflow's jet axis nearly halfway between its endpoints. We considered 265 these galaxies, J152933.03+601552.5 and J152932.16+601534.4, to be Porphyrion's host candidates. In 266 contrast to other radio-emitting structures along Porphyrion's axis, such as the southern complex inter-267 preted as an inner hotspot, these candidates have optical counterparts in Legacy Surveys DR10 imagery 268 (see Fig. 1's bottom panel inset). 269

¹Although Mpc-scale outflows are generated by galaxies, they are not galaxies themselves; therefore, referring to them as a class of 'galaxies' could cause confusion. In addition, Mpc-scale outflows may have been primarily studied through radio observations, but their synchrotron losses (like their other radiative losses) appear to have only a minor effect on their evolution [2], suggesting that 'radio' should not be used in a name meant to describe these objects intrinsically. Finally, while 'giant' appears apt, it is also vague; we thus prefer 'Mpc-scale'.

²Porphyrion was the son of Ouranos, the Greek primordial sky deity. According to Ps.-Apollodorus, he and Alcyoneus were the greatest of the Gigantes (Giants), while Pindar called him the 'king of the Giants'. He was struck by Zeus's thunderbolt in the Gigantomachy — the battle between the Giants and the Olympian gods for supremacy over the Cosmos.



Fig. 2.1: ILT image at central wavelength $\lambda = 2.08$ m, with a resolution of 19.8'', highlighting diffuse emission in the northern lobe and southern backflow. We show the same sky region and annotations as in Fig. 1. The contours denote 3σ , 5σ , and 10σ .

$_{270}$ uGMRT observations and data reduction

On 13 May 2023, we observed the outflow with the Upgraded Giant Metrewave Radio Telescope [uGMRT: 12] in Band 4 (550–750 MHz) for a total of 10 hours. On 23 September 2023, we extended these observations with another 5 hours. These observations are part of GMRT Observing Cycle 44 and have project 273 code 44_101. We requested to record both narrow-band (GSB) and wide-band (GWB) data. Adverse 274ionospheric conditions during the September run prohibited us from improving upon the images produced 275 with the May run data only. In what follows, we therefore exclusively discuss May run data reduction 276 and results. We performed calibration with Source Peeling and Atmospheric Modeling [SPAM; 13], start-277 ing out with the GSB data. After direction-dependent calibration, we used Python Blob Detection and 278 Source Finder [PyBDSF; 14] to derive a sky model from the final GSB image, which subsequently served 279 to initialise the direction-dependent calibration of the GWB data. As SPAM was designed with narrowband data in mind, following standard practice, we first split the GWB data along the frequency axis, 281 vielding four subbands of 50 MHz width each. We then calibrated each subband independently. A joint 282 image of four calibrated subbands revealed residual ionospheric artefacts from ILTJ153004.28+602423.2, 283 the same bright source in the vicinity of the northern lobe mentioned earlier. To mitigate these arte-284 facts, we subtracted (on a subband basis) all sources outside of a spherical cap with a 9' radius centred 285 around J2000 right ascension $\varphi = 15h29m32.0s$ and declination $\theta = 60d15m33.0s$. We then jointly reim-286 aged the four source-subtracted subbands with WSClean, using Briggs weighting 0. This resulted in the 287 4.3"-resolution image of Fig. 1's bottom panel. The noise level is $\sigma = 3$ Jy deg⁻² at its lowest. 288

In the Legacy Survey DR10 optical imagery shown in Fig. 1's bottom panel inset, we identified two 289 faint galaxies in the arcsecond-scale vicinity of the southern host galaxy candidate. Of these, the galaxy 290 at $(\varphi, \theta) = (232.37969^\circ, 60.26029^\circ)$ emits low-frequency radio emission at 6σ significance. At the 4.3" 291 resolution of our fiducial uGMRT image, this radio emission is only narrowly separable from the host 292 galaxy candidate's, thus interfering with establishing the radio morphology of the candidate. Trading 293 depth for resolution, we reimaged the uGMRT data with WSClean using Briggs weighting -0.5, yielding 294 a 3.6'' resolution. Subsequently, to isolate the radio morphology of J152932.16+601534.4, we fit a circular 295 Gaussian fixed at the sky coordinates of its radio-emitting neighbour. Naturally, we set this Gaussian's 296 full width at half maximum to 3.6". Upon subtracting the Gaussian, we obtained our final image; Fig. 2 297 shows its central region, where the noise level is $\sigma = 6$ Jy deg⁻² at its lowest. Only the southern (and 298



Fig. 2.2: Our ILT VLBI image of Porphyrion's central $3.84' \times 3.84'$ at $\lambda = 2.08$ m and 0.4''resolution covers a third of the total jet system and reveals two radio-luminous AGN, detected at $\sim 40\sigma$ significance. We show the overarching jet axis (translucent white), determined from the northern lobe and southern hotspot (not shown), to scale for a jet radius of 1 kpc. The jet axis appears to pass through J152932.16+601534.4.

most radio-luminous³) host galaxy candidate features an extension along the overarching jet axis seen 299 in Fig. 1. In our data, this extension — indicative of a pair of relativistically beamed jets — occurs at 300 5σ significance. 301

We estimated the probability to find a spurious (i.e. unrelated) radio-luminous AGN (RLAGN) with 302 jets along Porphyrion's overarching axis in the region where the host galaxy could plausibly reside. To find 303 the sky density of RLAGN with discernible jet orientations at arcsecond-scale resolutions, metre-scale 304 wavelengths, and 10^1 Jy deg⁻²-scale noise levels, we studied the LoTSS DR1-derived RLAGN sample 305 presented in Hardcastle et al. [16]. This sample, consisting of 23,344 RLAGN, contains 6,850 RLAGN 306 with discernible jet orientations. The latter population's average sky density $\bar{n}_s = 4 \cdot 10^{-3} \operatorname{arcmin}^{-2}$. 307 Approximating the sky density $n_{\rm s}$ of spurious RLAGN with discernible jet orientations near Porphyrion's 308 host with $\bar{n}_{\rm s}$ would be appropriate only if such RLAGN would not cluster in the sky. More optimally, 309 we estimated $n_{\rm s}$ by first counting, for each such RLAGN (that appears sufficiently far from the edges of 310 the survey footprint), the number of neighbours in disks of radius 1'. Next, we divided each count by the 311 solid angle of the disks, and finally determined the sample mean: $n_s = 8 \cdot 10^{-3} \operatorname{arcmin}^{-2}.^4$ We estimated 312 the solid angle of the 'strip' in which an unrelated source could be mistaken for Porphyrion's host to be 313 $\Omega_{\rm s} = 10^{0} \times 10^{-1}$ arcmin².⁵ Defining jets 'aligned' with Porphyrion's when their position angle falls within a 314 range of width 10^1 deg centred around Porphyrion's position angle, the probability of randomly attaining alignment $p_{\rm s} = \frac{10^{\circ}}{180^{\circ}} = 6 \cdot 10^{-2}$. One thus expects to encounter $\mathbb{E}[N_{\rm s}] = n_{\rm s} \cdot \Omega_{\rm s} \cdot p_{\rm s} = 4 \cdot 10^{-5}$ unrelated RLAGN with resolved and aligned jets near Porphyrion's host. Assuming that N_s is Poisson-distributed, one or more such spurious sources appear with a probability $\mathbb{P}(N_s \ge 1) = 1 - e^{-\mathbb{E}[N_s]} \approx \mathbb{E}[N_s]^{.6}$ We thus 317 318 find $\mathbb{P}(N_{\rm s} \ge 1) = 4 \cdot 10^{-5}$; the probability to find a spurious *unresolved* RLAGN in the same region is 319 $4 \cdot 10^1$ times larger. We conclude that J152932.16+601534.4 is Porphyrion's host galaxy.

³Radio luminosity L_{ν} is, at fixed redshift and large-scale halo mass, approximately proportional to jet power Q [2]. Under the Blandford–Znajek mechanism [15], $Q \propto M_{\bullet}^2$ (at fixed magnetic field strength and spin), where M_{\bullet} is the SMBH mass. As the generation of Porphyrion's jets entails a significant SMBH mass gain $\Delta M_{\bullet} \sim 10^8 - 10^9 M_{\odot}$, the SMBH must now be massive; hence, a high radio luminosity is expected.

For disks of larger radii, n_{e} approaches \bar{n}_{e} .

 $^{^{5}}$ We limited the strip's angular length by asserting that plausible host candidates lie between Porphyrion's two detected patches of jet emission. ⁶This approximation improves as $\mathbb{E}[N_s]$ decreases.



Fig. 2.3: Ultraviolet-optical rest-frame spectrum of J152933.03+601552.5, the quasarhosting galaxy 19" north-northeast of J152932.16+601534.4, Porphyrion's host galaxy. We identify redshifted hydrogen, carbon, oxygen, neon, and magnesium lines, jointly implying $z_s = 0.799 \pm 0.001$. Forbidden lines from the quasar's narrow-line region are shown in red. The spectrum has been measured with the LRIS on the W. M. Keck Observatory's Keck I Telescope.

321 Keck I observations and data reduction

The literature offers only photometric redshift estimates of the host galaxy. The SDSS DR12 [17] reports $z_{\rm p} = 0.68 \pm 0.06$, the Legacy Surveys DR9 [18] reports $z_{\rm p} = 0.93 \pm 0.08$, and Duncan [19] reports $z_{\rm p} = 0.92 \pm 0.08$. For radio-emitting galaxies like J152932.16+601534.4, we consider the latter estimate to be most reliable.

To establish the redshift of Porphyrion's host galaxy with certainty, we measured its (rest-frame) 326 ultraviolet-optical spectrum with the Low Resolution Imaging Spectrometer [LRIS; 20–23] on the W. M. Keck Observatory's Keck I Telescope. Adequate slit placement requires accurate knowledge of the galaxy's 328 coordinates. From the Legacy Surveys DR10 best-fit model, we found that J152932.16+601534.4's centre lies at $(\varphi, \theta) = (232.38410^\circ, 60.25960^\circ)$. The galaxy's half-light radius is 10.1 ± 0.3 kpc. On 23 June 330 2023, we observed the galaxy for a total of 900 seconds. We used the 600/4000 grism on LRIS' blue 331 side, with 1×2 binning (spatial and spectral, respectively), and the 400/8500 grating on the red side, 332 again with 1×2 binning. During the observations, the seeing was approximately 0.8''; as we used a 1.5''333 slit, minimal slit losses occurred. Using a slit position angle of -70° , we could simultaneously obtain a 334 spectrum for J152933.03+601552.5, the quasar-hosting galaxy which we initially considered (and then 335 discarded) as a host candidate. We reduced the data with PypeIt [24], a Python-based pipeline with features tailored to reducing LRIS long-slit spectroscopy. We flat-fielded and sky-subtracted the data 337 using standard techniques. We used internal arc lamps for wavelength calibration and a standard star 338 for overall flux calibration.

The final LRIS-derived spectra of J152932.16+601534.4 and J152933.03+601552.5 are shown in Figs. 3 and 2.3, respectively. The corresponding spectroscopic redshifts are $z_{\rm s} = 0.896 \pm 0.001$ and $z_{\rm s} = 0.799 \pm 0.001$. The uncertainties reflect LRIS' limited spectral resolution as well as systematic errors in wavelength calibration. The latter spectroscopic redshift can be compared to the value derived for J152933.03+601552.5 by the SDSS BOSS [25] on 5 July 2013. Visual inspection of the SDSS BOSS spectrum and its best fit indicates a robust spectroscopic redshift $z_{\rm s} = 0.79836 \pm 5 \cdot 10^{-5}$. The two measurements are in agreement.

347 Spectral energy distribution

To further assess the accretion mode of Porphyrion's AGN, and to estimate its host's stellar mass and possibly star formation rate (SFR), we performed spectral energy distribution (SED) inference. Through VizieR, the Astro Data Lab, and the NASA/IPAC Extragalactic Database, we collected catalogued total (rather than fixed-aperture) flux densities, relative flux densities, magnitudes, Galactic transmission fractions, and total extinctions from rest-frame ultraviolet to radio wavelengths. Figure 2.4 shows the crossmatching results. It demonstrates that Porphyrion's host galaxy (as identified in Legacy DR10) is,



Fig. 2.4: All flux densities used in the inference of Porphyrion's host galaxy SED occur within an arcsecond of the Legacy DR10-identified host position. Coloured disks show astrometric uncertainties, while grey circles denote angular distances from the Legacy DR10-identified host position. The golden stars mark all other Legacy DR10-identified sources in the angular vicinity of Porphyrion's host.

in view of the astrometric accuracies of the collected catalogue data, the only plausible match. Just 4.3''354 northeast from Porphyrion's host galaxy lies another source, which could be either a Milky Way star or 355 a galaxy. Mindful of the possibility of spuriously high flux density measurements as a result of target-356 neighbour blending, we assessed all images underlying the catalogued estimates by eye. The neighbouring source only appears to be a point of attention for flux density measurements at small wavelengths, 358 such as in the Legacy q- and r-band, where it has flux densities $\sim 100\%$ and $\sim 60\%$ those of the target, 359 respectively. At the Legacy z-band's larger wavelengths, the neighbour's flux density is small ($\sim 20\%$) 360 relative to the target's. The error induced by blending, which will add only a fraction of the neighbour's 361 flux density, should thus be negligible. Accordingly, the Pan-STARRS and WISE measurements at even 362 larger wavelengths are not compromised by this neighbour. 363

We converted the Legacy relative flux densities to flux densities by multiplying with the reference flux density $F_{\nu} = 3631$ Jy. We converted the Pan-STARRS AB magnitudes to flux densities using the standard relation (e.g. Eq. 1 of Chambers *et al.* [26]). We converted the WISE relative flux densities to flux densities by multiplying with the reference flux densities of Jarrett *et al.* [27]'s Table 1. Table 1 provides all retained flux densities F_{ν} and the central wavelengths λ they correspond to.

Porphyrion's host galaxy lies at a Galactic latitude $b = 47.43194^{\circ}$. Fortunately, at these latitudes, the Galactic transmission is high for all bands included in our SED inference. We tabulate estimated transmitted fractions f_t in Table 1. For Pan-STARRS *i* and *y*, we calculated f_t from total extinctions $A_{\lambda} = 0.022$ and $A_{\lambda} = 0.014$, respectively, via $f_t = 10^{-\frac{2}{5}A_{\lambda}}$. For Legacy *g*, where Galactic transmission is lowest, application of the correction factor f_t^{-1} results in a flux density increase of just ~4%. For all bands, the correction is smaller than the flux density uncertainty. We conclude that, for our purposes, Galactic extinction can be neglected.

³⁷⁶ Next, using AGNfitter [31, Martínez-Ramírez *et al.* in prep.], we determined the SED posterior shown ³⁷⁷ in the bottom panel of Fig. 3. The posterior indicates the presence of a luminous SMBH accretion disk ³⁷⁸ with an obscuring torus, confirming the radiatively efficient nature of Porphyrion's AGN. The SED ³⁷⁹ posterior further implies that the stellar mass of Porphyrion's host is $M_{\star} = 6.7 \pm 1.4 \cdot 10^{11} M_{\odot}$. To

Table 1: Flux densities F_{ν} of Porphyrion's host galaxy throughout the electromagnetic spectrum. These are as measured, and thus have not been corrected for Galactic extinction; to do so, we provide Galactic transmission fractions f_t . Entries are sorted by the central wavelengths λ of the observing bands.¹

Band	$\lambda~(\mu{ m m})$	$F_{ u}$ (Jy)	$f_{ m t}~(\%)$
Legacy g	$4.8 \cdot 10^{-1}$	$2.6 \pm 0.2 \cdot 10^{-6}$	96.3
Legacy r	$6.3 \cdot 10^{-1}$	$8.4 \pm 0.4 \cdot 10^{-6}$	97.5
Legacy z	$9.1 \cdot 10^{-1}$	$4.31 \pm 0.08 \cdot 10^{-5}$	98.6
Pan-STARRS <i>i</i>	$7.5 \cdot 10^{-1}$	$1.1 \pm 0.1 \cdot 10^{-5}$	98.0
Pan-STARRS y	$9.6 \cdot 10^{-1}$	$3.3 \pm 0.3 \cdot 10^{-5}$	98.7
WISE W1	$3.4\cdot 10^0$	$2.41 \pm 0.02 \cdot 10^{-4}$	99.8
WISE W2	$4.6\cdot 10^0$	$2.53 \pm 0.05 \cdot 10^{-4}$	99.9
WISE W3	$1.2\cdot 10^1$	$8.1 \pm 0.5 \cdot 10^{-4}$	100
WISE W4	$2.2\cdot 10^1$	$3.6 \pm 0.4 \cdot 10^{-3}$	100
VLASS	$1.0\cdot 10^5$	$1.4 \pm 0.2 \cdot 10^{-3}$	100
FIRST	$2.1\cdot 10^5$	$1.6 \pm 0.1 \cdot 10^{-3}$	100
uGMRT Band 4	$4.6\cdot 10^5$	$2.1 \pm 0.1 \cdot 10^{-3}$	100
LoTSS	$2.1\cdot 10^6$	$2.4 \pm 0.2 \cdot 10^{-3}$	100

¹ When multiple flux densities or magnitudes from the same band were available in literature catalogues, we picked the highest signal-to-noise ratio measurement. Legacy data come from Dey *et al.* [18], Pan-STARRS data from Chambers *et al.* [26], WISE data from Lang *et al.* [28], VLASS data from Gordon *et al.* [29], FIRST data from Helfand *et al.* [30], uGMRT data from the present work, and LoTSS data from Shimwell *et al.* [4].

gauge the sensitivity of stellar mass estimates for this galaxy to methodological variation, we compare our result to the corresponding stellar mass estimate in the LoTSS DR2 value-added catalogue [32]. This catalogue's authors derive a stellar mass $M_{\star} = 5.5^{+0.7}_{-0.6} \cdot 10^{11} M_{\odot}$ from SED fits to Legacy g, r, z and WISE W1 and W2 flux densities.⁷ The two stellar mass measurements are in agreement. Due to the lack of rest-frame far-infrared photometry, the SFR of Porphyrion's host is virtually unconstrained by the

385 SED posterior.

Radio luminosities and spectral indices

To determine metre-wavelength radio luminosities and a metre-wavelength spectral index for Porphyrion, we first measured its flux densities in the 6.2" ILT and 4.3" uGMRT images. We assumed flux scale uncertainties of 10% and 5%, respectively.

Summing over all structural components, the outflow's total flux density at $\lambda = 2.08$ m is $F_{\nu} =$ 390 63 ± 6 mJy. Its total radio luminosity at rest-frame wavelength $\lambda_r = 1.10$ m therefore is $L_{\nu} = 1.4 \pm 0.1$. 391 10^{26} W Hz⁻¹; the core radio luminosity, $L_{\nu} = 5.3 \pm 0.5 \cdot 10^{24}$ W Hz⁻¹, comprises ~4% of the total. The 392 outflow's total flux density at $\lambda = 0.46$ m is $F_{\nu} = 12.0 \pm 0.6$ mJy. Its total radio luminosity at $\lambda_{\rm r} = 0.24$ m therefore is $L_{\nu} = 2.7 \pm 0.1 \cdot 10^{25}$ W Hz⁻¹; the core radio luminosity, $L_{\nu} = 4.7 \pm 0.2 \cdot 10^{24}$ W Hz⁻¹, 393 394 comprises $\sim 17\%$ of the total. These data imply a metre-wavelength total spectral index $\alpha = -1.09 \pm 0.08$ 395 and a core spectral index $\alpha = -0.09^{+0.08}_{-0.07}$. Through spectral index-based interpolation, we estimated the 396 total radio luminosity at $\lambda_{\rm r} = 2$ m to be $L_{\nu} = 2.8 \pm 0.3 \cdot 10^{26}$ W Hz⁻¹. This latter total radio luminosity 397 is an important input for our dynamical modelling. 398

We calculated directionally resolved metre-wavelength spectral indices by combining the ILT and 399 uGMRT images. Before doing so, we convolved the latter image to the former's resolution. In Fig. 2.5, we 400 show two regions of interest from the resulting spectral index map, which consequently has a resolution 401 of 6.2''. To highlight the directions in which our spectral index measurements are informative, we blanked 402 all directions in which the thermal noise-induced spectral index uncertainty exceeds 0.3. The top panel 403 of Fig. 2.5 shows that J152932.16+601534.4, Porphyrion's host galaxy, has a significantly higher spectral 404 index than J152933.03+601552.5, the aforementioned quasar-hosting galaxy. The former spectral index 405 is consistent with zero, indicating that the onset of synchrotron self-absorption (SSA) in Porphyrion's 406 host galaxy occurs at metre wavelengths. By contrast, the onset of SSA in the quasar-hosting galaxy 407 must occur at longer wavelengths, suggesting a lower lepton energy density and weaker magnetic fields 408 in its synchrotron-radiating region. The bottom panel of Fig. 2.5 shows that Porphyrion's southern tip 409 features much lower spectral indices, with a gradient along the jet axis. This gradient is consistent with 410 a scenario of a hotspot with backflow in which spectral ageing occurs. Whereas $\alpha = -1.0 \pm 0.2$ at the 411 hotspot's southwestern side, the radio spectra gradually steepen to $\alpha = -1.6 \pm 0.2$ at the hotspot's 412 northeastern side. No spectral trend appears present further downstream. 413

⁷This stellar mass estimate is not based on the spectroscopic redshift we have obtained through LRIS, but utilises a photometrybased redshift posterior with mean and standard deviation $z_{\rm p} = 0.92 \pm 0.08$ [19].



Fig. 2.5: Metre-wavelength spectral indices around Porphyrion's centre and southern tip. The top panel, which covers $3' \times 3'$, reveals synchrotron self-absorption at metre wavelengths in the host galaxy, consistent with the fuelling of powerful jets. The bottom panel, which covers $2' \times 2'$, reveals a hotspot with backflow. We show the mean spectral index α between 0.46–2.08 m, at a resolution of 6.2". From light to dark, the contours denote thermal noise–induced spectral index uncertainties of 0.05, 0.1, 0.2, and 0.3.

We investigated further whether the spectral index discrepancy between J152932.16+601534.4 and 414 J152933.03+601552.5 constitutes evidence that the former galaxy is Porphyrion's host. For each of the 415 $1.1 \cdot 10^4$ Mpc-scale outflows catalogued by Mostert *et al.* [33], we determined LoTSS DR2 and VLASS 416 core flux densities. LoTSS DR2 core flux densities were available for 1,238 Mpc-scale outflows, whilst 417 VLASS core flux densities were available for 6,882. We found 924 Mpc-scale outflows for which both 418 core flux densities were available and computed the corresponding 144 MHz–3 GHz spectral indices. The 419 results are summarised in Fig. 2.6. It is likely that some VLASS-detected cores remain undetected in 420 LoTSS DR2, in particular if they have flat or 'inverted' spectra. The result is a bias in Fig. 2.6 towards 421



Fig. 2.6: LoTSS–VLASS spectral index distribution of the cores of 924 Mpc-scale outflows. In grey, we indicate the bins in which the core spectral indices of J152932.16+601534.4, Porphyrion's claimed host galaxy, and J152933.03+601552.5 fall. The distribution suggests that the core spectral index of J152932.16+601534.4 is more typical for Mpc-scale outflows than the core spectral index of J152933.03+601552.5. For J152933.03+601552.5, due to a VLASS non-detection, we show the LoTSS–uGMRT Band 4 spectral index.

lower spectral indices. In addition, by requiring that the LoTSS DR2–detected core is an isolated source
on the sky, the core spectral indices of Fanaroff–Riley I–like outflows have likely been selected out. As
Porphyrion is a Fanaroff–Riley II outflow, this deselection of Fanaroff–Riley I outflows makes the distribution arguably more representative. The spectral indices in this sample do not show an obvious trend with
redshift. From Fig. 2.6, we conclude that the known core spectral indices of Mpc-scale outflows favour
J152932.16+601534.4 over J152933.03+601552.5 as Porphyrion's host, strengthening our identification.

428 Cosmic Web environment

Cosmic Web environment characterisations of luminous $(L_{\nu}(\nu = 150 \text{ MHz}) \ge 10^{24} \text{ W Hz}^{-1})$ Mpc-scale 429 outflows in the Local Universe ($z \leq 0.2$) have recently been obtained [34] by localisation in Bayesian 430 large-scale structure reconstructions and by crossmatching with catalogues of galaxy clusters ($M_{500} \ge 0.6 \cdot 10^{14} M_{\odot}$) and galaxy groups ($M_{500} < 0.6 \cdot 10^{14} M_{\odot}$). The resulting probability distribution over 431 432 Cosmic Web environments serves as a prior distribution for Porphyrion's Cosmic Web environment. In 433 the Local Universe, $\sim 30\%$ of all luminous Mpc-scale outflows reside in clusters, $\sim 60\%$ in groups, and the 434 remaining $\sim 10\%$ in more dilute parts of filaments, in sheets, or in voids [34]. Thus, if this probability 435 distribution does not evolve with redshift and a cluster environment can be excluded, Porphyrion likely originates from a filament. To evaluate whether Porphyrion's host galaxy inhabits a cluster, we extracted right ascensions, declinations, redshifts, and R_{500} -radii from the cluster catalogue of Wen & Han [35], 438 which is based on Legacy DR10. Even though these data allow for cluster detections up to $z \sim 1.5$, we 439 did not find a cluster close to Porphyrion's host. To reach this conclusion statistically, we first estimated 440 cluster redshift uncertainties using $\sigma_z(z) = 0.02 \cdot \frac{z}{0.9} \cdot (1+z)$ for photometric cluster redshifts, as suggested by the bottom-right panel of Fig. 7 of Wen & Han [35], and $\sigma_z = 0.001$ for spectroscopic cluster redshifts. 441 442 We neglected uncertainties in cluster right ascensions and declinations. We then Monte Carlo-simulated a 443 redshift for both Porphyrion's host and all clusters (assuming Gaussian redshift distributions), converted 444 right ascensions, declinations, and redshifts into comoving coordinates, and finally identified the cluster 445 nearest to Porphyrion's host. We recorded the comoving distance to this cluster as well as the ratio 446 between the corresponding proper distance and the cluster's R_{500} -radius. We repeated this Monte Carlo 447 procedure millions of times, until the probability distributions over these distance measures converged. 448 The results are shown in Fig. 2.7. Around Porphyrion's redshift, the Wen & Han [35] photometric cluster 449 redshift uncertainties $\sigma_z \approx 0.04$, large enough to force us to consider several clusters as candidates for 450 being the nearest. Each peak corresponds to the smallest possible distance to a possibly nearest cluster. 451 The peak location is determined by both the angle between Porphyrion's host and the cluster and by Porphyrion's redshift. In Monte Carlo realisations such that the cluster redshift matches Porphyrion's, 453 the distance is minimal. The nearest cluster lies at a comoving distance of 30^{+12}_{-17} Mpc, or 31^{+14}_{-16} cluster 454



Fig. 2.7: DESI Legacy Imaging Surveys DR10 galaxy cluster redshift uncertainties induce multimodal, asymmetric probability distributions over measures of distance between Porphyrion's host galaxy and the nearest galaxy cluster. We mark median-centred intervals containing 68% and 95% of all probability. The data suggest that Porphyrion does not originate from a cluster.

radii (68% probability intervals); the nearest cluster lies at a comoving distance of 30^{+14}_{-22} Mpc, or 31^{+19}_{-23} cluster radii (95% probability intervals). In just 0.1% of all realisations, Porphyrion's host is five or fewer R_{500} -radii away from the nearest cluster.

To investigate whether a filament or a void environment is more probable, we performed probabilistic 458 galaxy counts using the Legacy data underlying the Wen & Han [35] cluster catalogue. We extracted 459 right ascensions, declinations, redshift posterior means, and redshift posterior standard deviations of all 460 Legacy-detected galaxies that lie within 1.5° of Porphyrion's host. In a similar spirit as before, we then 461 Monte Carlo-simulated redshifts (where, for simplicity, we approximated the galaxies' redshift posterior 462 distributions with Gaussian distributions), converted right ascensions, declinations, and redshifts into 463 comoving coordinates, and counted the number of Legacy-detected galaxies (excluding Porphyrion's 464 host) within a sphere of given radius centred around Porphyrion's host. To properly take into account 465 galactic redshift uncertainties, we repeated this Monte Carlo procedure 1,000 times. In a sphere with a 466 comoving radius of 10 Mpc centred around Porphyrion's host, we counted 35 ± 6 other Legacy-detected 467 galaxies. We then performed analogous probabilistic galactic neighbour counts for a control sample of 468 galaxies at comparable redshifts. We selected controls by demanding that their redshift means do not 469 deviate more than 0.05 from Porphyrion's. To ensure that these mean redshifts are reliable, we further 470 demanded that the redshift standard deviations of controls are less than 0.1. From the available candidate 471 controls, we picked 100 controls at random, and performed the counts for them. Porphyrion's galactic 472 neighbour count, relative to those of the control sample, occurs at percentile 42^{+26}_{-23} %. If we assume 473

that circumgalactic Cosmic Web density is a monotonic function of the number of galactic neighbours, Porphyrion's circumgalactic Cosmic Web density percentile will be $42^{+26}_{-23}\%$, too. This suggests that Porphyrion does not originate from a void. In line with the expectation for luminous Mpc-scale outflows

⁴⁷⁷ in the Local Universe, we conclude that Porphyrion most likely originates from a filament.

478 Dynamical modelling: jet power and age

We derived Porphyrion's jet power and age from its length, radio luminosity, cosmological redshift, and likely environment by fitting evolutionary tracks. We generated these evolutionary tracks with the 480 simulation-based analytic outflow model of Hardcastle [2]. This model requires assumptions on the large-481 scale environment in which the dynamics take place. Following the previous section, we suppose that 482 the host galaxy resides in the centre of a galaxy group of mass $M_{500} = 10^{13} M_{\odot}$ (which comprises 483 contributions from both dark and baryonic matter) [34, 36]. We assigned the group a universal pressure 484 profile [UPP; 37] $p_{\rm g}(r)$,⁸ which can be parametrised just by M_{500} . To obtain the group's baryon density 485 profile from its pressure profile, we invoked the ideal gas law: $\rho_{\rm g}(r) = \frac{p_{\rm g}(r)\langle m \rangle}{k_{\rm B}T_{\rm g}}$, where $\langle m \rangle$ is the average plasma particle mass and $T_{\rm g}$ the group temperature. We assumed a pure ¹H-⁴He plasma with a ⁴He mass fraction Y = 25% [e.g. 39], so that $\langle m \rangle \approx \frac{4}{8-5Y}m_{\rm p} = 0.6 m_{\rm p}$, where $m_{\rm p}$ is the proton mass. 487 488 We estimated $T_{\rm g}$, which we assumed constant in space and time, using the mass-temperature relation 489 specified by Eq. 9 and Tables 3 and 4 of Lovisari *et al.* [40]: 490

$$\frac{k_{\rm B}T_{\rm g}}{2\,{\rm keV}} = 0.77 \cdot \left(\frac{M_{500}}{5 \cdot 10^{13} \ h_{70}^{-1} \ M_{\odot}}\right)^{0.61}.$$
(1)

The aforementioned mass implies $T_{\rm g} = 7 \cdot 10^6$ K. As Mpc-scale outflows reach beyond the edges of 491 groups, it was also necessary to estimate the pressure and baryon density in the AGN's more distant 492 surroundings. Following the bottom-right panel of Ricciardelli et al. [41]'s Fig. 6, we set the baryon 493 overdensity within voids at Porphyrion's redshift to $\delta = -0.7.9$ We obtained a void baryon density 494 $\rho_{\rm v} = \rho_{\rm c,0} \Omega_{\rm BM,0} (1+z)^3 (1+\delta) = 9 \cdot 10^{-31} \text{ g cm}^{-3}$, where $\rho_{\rm c,0}$ is today's critical density. Following Upton 495 Sanderbeck et al. [42]'s detailed study of IGM temperatures through cosmic time, which suggests a void 496 temperature $T_{\rm v} \sim 10^3 - 10^4$ K at Porphyrion's redshift, we set $T_{\rm v} = 1 \cdot 10^4$ K. This choice reflects the 497 fact that we are interested in void temperatures near the galaxy group. Again applying the ideal gas 498 law, and taking $\langle m \rangle$ as before, we obtained a void pressure $p_v = 1 \cdot 10^{-19}$ Pa. Finally, we defined the 499 external pressure $p_{\rm e}(r) = p_{\rm g}(r) + p_{\rm v}$, baryon density $\rho_{\rm e}(r) = \rho_{\rm g}(r) + \rho_{\rm v}$, and baryon density–weighted temperature $T_{\rm e}(r) = \frac{\rho_{\rm g}(r)T_{\rm g} + \rho_{\rm v}T_{\rm v}}{\rho_{\rm e}(r)}$. Figure 2.8 shows these profiles. 500 501

We explored whether the addition of a filament component would significantly change Fig. 2.8's profiles. We assumed a baryon overdensity $\delta = 10$ at the filament spine, and baryon density and temperature profiles following Tuominen *et al.* [43]'s results for massive filaments in the EAGLE simulation. We found pressure and baryon density contributions of an importance similar to or lesser than that of the group, even at Mpc-scale distances. We thus considered the addition of the filament unnecessary, especially in light of model uncertainties such as the group's mass and the surmised validity of extrapolating the group's UPP to Mpc-scale distances.

We generated 21 evolutionary tracks of 200 time steps each, spanning a range jet powers $Q = 10^{38.8}$ $10^{39.2}$ W. Propagating total length and radio luminosity uncertainties, we obtained $Q = 1.3 \pm 0.1 \cdot 10^{39}$ W 510 and $T = 1.9^{+0.7}_{-0.2}$ Gyr. The outflow's jet power uncertainty is set by radio luminosity uncertainty while 511 its age uncertainty is set by total length uncertainty. The inferred Gyr-scale age suggests that treating outflow evolution as a process at a single redshift — as is currently done in the model of Hardcastle [2] 513 — is crude for the largest outflows, and may need revision. Each jet's average speed $\langle \beta \rangle \coloneqq \frac{\langle v \rangle}{2cT} = \frac{l}{2cT} = 0.58^{+0.04}_{-0.07}\%$, where c is the speed of light. The energy transported by the jets $E = QT = 7.6^{+2.1}_{-0.7} \cdot 10^{55}$ J. As 514 515 a black hole can redirect at most half of the rest energy of infalling matter to electromagnetic radiation and jet fuelling, and the energy an RE AGN spends on electromagnetic radiation must at least equal 517 the energy spent on jet fuelling, the black hole must have gained a mass $\Delta M_{\bullet} > 2\frac{E}{c^2} = 8.5^{+2.4}_{-0.8} \cdot 10^8 M_{\odot}$ 518 while powering the jets. 519

⁸Sun *et al.* [38] have shown that the UPP applies to galaxy groups, even though the profile has originally been proposed to fit data on galaxy *clusters* (which have much higher masses: $10^{14} M_{\odot} < M_{500} < 10^{15} M_{\odot}$). ⁹In doing so, we implicitly assumed that the baryonic matter overdensity field is identical to the total matter overdensity field

^oIn doing so, we implicitly assumed that the baryonic matter overdensity field is identical to the total matter overdensity field (which comprises contributions from both dark and baryonic matter), as Ricciardelli *et al.* [41] considers the latter.



Fig. 2.8: Pressure, baryon density, and temperature external to the outflow, as a function of the proper distance from Porphyrion's AGN, in our dynamical modelling. The profiles consist of contributions from the outflow's presumed galaxy group and the adjacent voids.

520 Total outflow length

To estimate Porphyrion's total length from its projected length, we perform statistical deprojection. Equation 9 of Oei *et al.* [44] stipulates the probability density function (PDF) of an outflow's total length random variable (RV) L in case its projected length RV $L_{\rm p}$ is known to equal some value $l_{\rm p}$. This PDF is parametrised by the tail index ξ of the Pareto distribution assumed to describe L. We calculate the median and expectation value of $L \mid L_{\rm p} = l_{\rm p}$ for tail indices $\xi = -3$ and $\xi = -4$, the integer values closest to the observationally favoured $\xi = -3.5 \pm 0.5$ [44].

First, we determine the cumulative distribution function (CDF) of $L \mid L_{\rm p} = l_{\rm p}$ through integration:

$$F_{L|L_{p}=l_{p}}(l) \coloneqq \int_{-\infty}^{l} f_{L|L_{p}=l_{p}}(l') \, \mathrm{d}l'$$

$$= \frac{-\xi}{2^{1+\xi}\pi} \frac{\Gamma^{2}\left(-\frac{\xi}{2}\right)}{\Gamma(-\xi)} \int_{1}^{\max\{x,1\}} \frac{x'^{\xi-1}}{\sqrt{x'^{2}-1}} \, \mathrm{d}x',$$
(2)

where $x := \frac{l}{l_{p}}$ and $x' := \frac{l'}{l_{p}}$. For $\xi = -3$, the CDF concretises to

$$F_{L|L_{p}=l_{p}}(l) = \frac{3}{2} \int_{1}^{\max\{x,1\}} \frac{\mathrm{d}x'}{x'^{4}\sqrt{x'^{2}-1}}$$

$$= \begin{cases} 0 & \text{if } x < 1; \\ \frac{(2x^{2}+1)\sqrt{x^{2}-1}}{2x^{3}} & \text{if } x \ge 1. \end{cases}$$
(3)

The median conditional total length, $l_{\rm m}$, is defined by $F_{L|L_{\rm p}=l_{\rm p}}(l_{\rm m}) \coloneqq \frac{1}{2}$. Numerically, we obtain $x_{\rm m} \coloneqq \frac{l_{\rm m}}{l_{\rm p}} \approx 1.0664$, or $l_{\rm m} \approx 1.0664 l_{\rm p}$. As $l_{\rm p} = 6.43 \pm 0.05$ Mpc, we find $l_{\rm m} = 6.86 \pm 0.05$ Mpc. An analogous numerical determination of the 16-th and 84-th percentiles then yields $l = 6.9^{+1.6}_{-0.4}$ Mpc.

533 For $\xi = -4$, the CDF concretises to

$$F_{L|L_{p}=l_{p}}(l) = \frac{16}{3\pi} \int_{1}^{\max\{x,1\}} \frac{\mathrm{d}x'}{x'^{5}\sqrt{x'^{2}-1}}$$

$$= \begin{cases} 0 & \text{if } x < 1; \\ \frac{2}{3\pi} \left(\frac{(3x^{2}+2)\sqrt{x^{2}-1}}{x^{4}} + 3\arccos\frac{1}{x}\right) & \text{if } x \ge 1. \end{cases}$$

$$(4)$$

Numerically, we obtain $x_{\rm m} \approx 1.0515$, or $l_{\rm m} \approx 1.0515 l_{\rm p}$, and thus $l_{\rm m} = 6.76 \pm 0.05$ Mpc. In the same way as before, we find $l = 6.8^{+1.2}_{-0.3}$ Mpc.

Equation 10 of Oei *et al.* [44] gives a closed-form expression for $\mathbb{E}[L \mid L_{\rm p} = l_{\rm p}](\xi)$. Table 1 of the same work lists $\mathbb{E}[L \mid L_{\rm p} = l_{\rm p}](\xi = -3) = \frac{3\pi}{8}l_{\rm p}$ and $\mathbb{E}[L \mid L_{\rm p} = l_{\rm p}](\xi = -4) = \frac{32}{9\pi}l_{\rm p}$. In the case of Porphyrion, these expressions concretise to $\mathbb{E}[L \mid L_{\rm p} = l_{\rm p}](\xi = -3) = 7.58 \pm 0.06$ Mpc and $\mathbb{E}[L \mid L_{\rm p} = l_{\rm p}](\xi = -4) = \frac{32}{9\pi}l_{\rm p}$.

⁵⁴⁰ By conditioning L on more knowledge than a value for L_p alone, statistical deprojection could be made ⁵⁴¹ more precise. For example, one could additionally condition on the fact that Porphyrion is generated ⁵⁴² by a Type 2 radiatively efficient (RE) AGN. If Type 1 RE AGN are seen mostly face-on and Type 2 ⁵⁴³ RE AGN are seen mostly edge-on, as proposed by the unification model [e.g. 45], then the detection of ⁵⁴⁴ a Type 2 RE AGN would imply that the jets make a small angle with the sky plane. Extending the ⁵⁴⁵ formulae to include this knowledge is beyond the scope of this work; however, mindful of the associated ⁵⁴⁶ deprojection factor-reducing effect, we choose $\xi = -4$ as our fiducial tail index.

To assess Porphyrion's transport capabilities in a cosmological context, it is instructive to calculate its length relative to Cosmic Web length scales. In particular, the outflow's total length relative to the typical cosmic void radius at its epoch is $f_{\rm v} := l(1+z)R_{\rm v}^{-1}$, where $R_{\rm v}$ is the typical comoving cosmic void radius. For $l = 6.8^{+1.2}_{-0.3}$ Mpc, $z = 0.896 \pm 0.001$, and $R_{\rm v} = 20$ Mpc [46], we find $f_{\rm v} = 64^{+12}_{-2}$ %. For our fiducial total length l = 7 Mpc, we find $f_{\rm v} = 66\%$.

552 Filament shape modification

We predict that powerful, long-lived outflows like Porphyrion cause their host galaxies' filaments to expand thermally. Through lateral shocks, the jets distribute an amount of heat Q_{WHIM} over the warmhot IGM. This medium is sufficiently dilute that plasma interactions can be neglected; as a result, the ideal gas law, $pV = Nk_{\rm B}T$, may be adopted as the equation of state. Here, p, V, N, and T are the filament's pressure, volume, plasma particle number, and temperature, respectively; $k_{\rm B}$ is Boltzmann's constant. Assuming a thermodynamic process at constant pressure and particle number, the work W is

$$W = p\Delta V = Nk_{\rm B}\Delta T.$$
(5)

⁵⁵⁹ Before the outflow's emergence, the filament's equation of state is $pV_i = Nk_BT_i$, where V_i and T_i are its ⁵⁶⁰ initial volume and temperature, respectively. Upon dividing Eq. 5 by this equation of state, one obtains

$$\frac{\Delta V}{V_{\rm i}} = \frac{\Delta T}{T_{\rm i}}.\tag{6}$$

Assuming that the filament retains a cylindrical shape, initially with radius r_i and finally with radius r_f , and using that $\Delta V \coloneqq V_f - V_i$, one obtains

$$\frac{r_{\rm f}}{r_{\rm i}} = \sqrt{1 + \frac{\Delta T}{T_{\rm i}}}.\tag{7}$$

The radius ratio, $\frac{r_{\rm f}}{r_{\rm i}}$, depends only on the ratio between the temperature increase $\Delta T \coloneqq T_{\rm f} - T_{\rm i}$ and the initial temperature. The temperature increase is

$$\Delta T = \frac{Q_{\rm WHIM}}{NC_{\rm p,m}},\tag{8}$$

where $C_{p,m}$ is the molar heat capacity at constant pressure. For a monatomic gas or a hydrogen plasma, $C_{p,m} = \frac{5}{2}R$, where R is the molar gas constant. The number of filamentary electrons and atomic nuclei affected by the outflow is

$$N = \frac{\pi r_{\rm i}^2 L \rho_{\rm i}}{\mu m_{\rm p}},\tag{9}$$

where L is the length of the cylindrical segment affected, ρ_i is the initial baryonic mass density, μ is the average mass of a plasma particle relative to the proton mass, and m_p is the proton mass. We estimate $\frac{L}{2}$ by multiplying the typical speed of lateral shocks with the outflow's lifetime. We decompose $\rho_i = \rho_{c,0}\Omega_{BM,0}(1+z)^3(1+\delta)$, where z and δ are the filament's cosmological redshift and baryonic overdensity, respectively.

To estimate Q_{WHIM} given E, the total energy carried by the jets up to the time of observation, we turn to analytical models and numerical simulations. Modelling indicates that just $\sim 10\%$ of the total energy 574 is lost through radiative processes [2]. This fraction increases with redshift, as inverse-Compton losses to 575 the CMB become more pronounced. Numerical simulations show that, at least in galaxy clusters, $\sim 50\%$ of the non-radiated energy is converted into thermal or kinetic energy carried by the shocked medium, and the other $\sim 50\%$ is converted into thermal or kinetic energy carried by the outflow's lobes [47]. Over 578 time, the kinetic energy turns into thermal energy. It is, at present, unclear how fast remnant lobes mix 579 with the surrounding medium, and how the mixing timescale varies with the latter's density. Here we 580 assume that, at late times, all of the lobes' energy mixes with the surrounding medium. As such, we 581 estimate $Q_{\text{WHIM}} \rightarrow 90\% \cdot E$. 582

⁵⁸³ We assess the outflow-induced morphological change to Porphyrion's filament by evaluating Eq. 7, ⁵⁸⁴ taking $Q_{\text{WHIM}} = 7 \cdot 10^{55}$ J, $r_i \approx r_c = 1.2$ Mpc (a typical filament core radius [43]), $L = 2 \cdot 7$ Mpc = 14 Mpc ⁵⁸⁵ (assuming that the region beyond the outflow's direct reach that is affected at late times is comparable ⁵⁸⁶ in length to the outflow itself), z = 0.9, $1 + \delta = 10$, $\mu = 0.5$, and $T_i = 10^7$ K; we find $\Delta T = 3 \cdot 10^7$ K (an ⁵⁸⁷ increase of ~300%) and $r_f = 2.4$ Mpc (an increase of ~100%). Porphyrion's heat dissipation renders the ⁵⁸⁸ outflow's native filament much hotter and thicker than it would have otherwise been.

For our cosmological outlook, we assumed a typical jet power and age that are each an order of magnitude lower than Porphyrion's. We thus estimated the combined energy carried by 10 Mpc-scale outflows to be $Q_{\text{WHIM}} = 7 \cdot 10^{54}$ J. Assuming non-overlapping affected regions, we estimated $L = 10 \cdot 2 \cdot 1$ Mpc = 20 Mpc. Leaving all other parameters identical, we find $\Delta T = 2 \cdot 10^6$ K (an increase of ~20%) and $r_{\text{f}} = 1.3$ Mpc (an increase of ~10%).

594 Quasar mass-based host galaxy candidate elimination

SDSS J152933.03+601552.5 is the quasar-hosting galaxy 19" north-northeast of J152932.16+601534.4, the galaxy we have identified as Porphyrion's host. We initially also considered SDSS J152933.03+601552.5 as a host galaxy candidate. However, aforementioned arguments involving the presence of jets and their orientation and, to a lesser degree, arguments involving core radio luminosity and core synchrotron self-absorption all favour J152932.16+601534.4. We now discuss how our results would change if, instead, SDSS J152933.03+601552.5 were Porphyrion's host galaxy. Doing so will lead to a contradiction that disproves this alternative hypothesis.

First, we discuss results that do not require dynamical modelling. To start with, Porphyrion would 602 remain generated by an RE AGN. The host galaxy redshift would decrease from $z = 0.896 \pm 0.001$ to z =603 0.799 ± 0.001 , decreasing Porphyrion's projected length from $l_{\rm p} = 6.43 \pm 0.05$ Mpc to $l_{\rm p} = 6.21 \pm 0.05$ Mpc. Again using $\xi = -4$, the total length would decrease from $l = 6.8^{+1.2}_{-0.3}$ Mpc to $l = 6.5^{+1.2}_{-0.3}$ Mpc and its 605 conditional expectation from $\mathbb{E}[L \mid L_{\rm p} = l_{\rm p}] = 7.28 \pm 0.05$ Mpc to $\mathbb{E}[L \mid L_{\rm p} = l_{\rm p}] = 7.03 \pm 0.06$ Mpc. If orientation distinguishes Type 1 from Type 2 RE AGN, as the unification model supposes, then 607 these statistical deprojection results may underestimate Porphyrion's total length. Porphyrion would 608 remain the projectively longest galaxy-made structure identified so far. The host's stellar mass would 609 decrease from $M_{\star} = 6.7 \pm 1.4 \cdot 10^{11} M_{\odot}$ to $M_{\star} = 4.0^{+0.3}_{-0.3} \cdot 10^{11} M_{\odot}$, while the SFR would become $S = 4.9^{+0.3}_{-0.4} \cdot 10^1 M_{\odot}$ yr⁻¹ [48]. Porphyrion's total radio luminosity at rest-frame wavelength $\lambda_{\rm r} = 2$ m would decrease from $L_{\nu} = 2.8 \pm 0.3 \cdot 10^{26}$ W Hz⁻¹ to $L_{\nu} = 2.2 \pm 0.2 \cdot 10^{26}$ W Hz⁻¹. 610 611 612

Next, we discuss results that come from dynamical modelling. The jet power would decrease from $Q = 1.3 \pm 0.1 \cdot 10^{39}$ W to $Q = 1.0 \pm 0.1 \cdot 10^{39}$ W, while the age would slightly increase from $T = 1.9^{+0.7}_{-0.2}$ Gyr to $T = 1.9^{+0.7}_{-0.1}$ Gyr. The transported energy would decrease from $E = 7.6^{+2.1}_{-0.7} \cdot 10^{55}$ J to $E = 6.4^{+1.8}_{-0.6} \cdot 10^{55}$ J, and the minimum black hole mass gain from $\Delta M_{\bullet} > 8.5^{+2.4}_{-0.8} \cdot 10^8$ M_{\odot} to $\Delta M_{\bullet} > 7.2^{+2.0}_{-0.7} \cdot 10^8$ M_{\odot} .

Finally, we arrive at a contradiction, as the quasar's SMBH mass (measured from its SDSS BOSS spectrum) $M_{\bullet} = 2.5 \pm 0.3 \cdot 10^8 M_{\odot}$ [49]. This mass is lower than the minimum mass gain associated to the fuelling of Porphyrion's jets. Thus, assuming that SDSS J152933.03+601552.5 is the outflow's host galaxy leads to a contradiction. This argument reaffirms that J152932.16+601534.4 is Porphyrion's host.

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Data availability. The LoTSS DR2 is publicly available at https://lofar-surveys.org/dr2_release.html. The authors will share the particular LOFAR, uGMRT, and Keck I Telescope data used in this work upon request.

Code availability. The dynamical model used to interpret the outflow is described by Hardcastle [2] and available for download at https://github.com/mhardcastle/analytic. Analysis and plotting code specific to this work is available [50] on Code Ocean: https://codeocean.com/capsule/3908804/tree.

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provided comments to improve the text. 665

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References 669

- Planck Collaboration et al. Planck 2018 results. VI. Cosmological parameters. A&A 641, A6 (2020) 670
- 671 Hardcastle, M. J. A simulation-based analytic model of radio galaxies. MNRAS 475, 2768–2786 (2018)
- 3. 672
- 673 4.
- Shimwell, T. W. et al. LOFAR Two-metre Sky Survey. V. Second data release. A&A 659, A1 (2022).
 Shimwell, T. W. et al. The LOFAR Two-metre Sky Survey. I. Survey description and preliminary data release. A&A 598, 674 5.A104 (2017).
- 6. Tasse, C. et al. DDFacet: Facet-based radio imaging package Astrophysics Source Code Library, record ascl:2305.008. 2023. 676 677 7van Weeren, R. J. et al. LOFAR observations of galaxy clusters in HETDEX. Extraction and self-calibration of individual 678 LOFAR targets. A&A 651, A115 (2021).
- 8. Offringa, A. R. et al. WSCLEAN: an implementation of a fast, generic wide-field imager for radio astronomy. MNRAS 444, 679 606-619 (2014) 680
- 9 Morabito, L. K. et al. Sub-arcsecond imaging with the International LOFAR Telescope. I. Foundational calibration strategy 681 and pipeline. A&A 658, A1 (2022). 682
- Jackson, N. et al. LBCS: The LOFAR Long-Baseline Calibrator Survey. A&A 595, A86 (2016) 683 10.
- Jackson, N. *et al.* Sub-arcsecond imaging with the International LOFAR Telescope. II. Completion of the LOFAR Long-Baseline Calibrator Survey. A&A **658**, A2 (2022). 684 11. 685 12
- Gupta, Y. et al. The upgraded GMRT: opening new windows on the radio Universe. Current Science 113, 707-714 (2017). 686 Intema, H. T. SPAM: Source Peeling and Atmospheric Modeling Astrophysics Source Code Library, record ascl:1408.006. 687 13. 2014.688
- Mohan, N. & Rafferty, D. PyBDSF: Python Blob Detection and Source Finder Astrophysics Source Code Library, record 689 14.ascl:1502.007. 2015.
- Blandford, R. D. & Znajek, R. L. Electromagnetic extraction of energy from Kerr black holes. MNRAS 179, 433–456 (1977). 15 691 16.Hardcastle, M. J. et al. Radio-loud AGN in the first LoTSS data release. The lifetimes and environmental impact of jet-driven sources. A&A 622, A12 (2019).
- Alam, S. et al. The Eleventh and Twelfth Data Releases of the Sloan Digital Sky Survey: Final Data from SDSS-III. ApJS 694 17. **219**, 12 (2015)
- 18 Dey, A. et al. Overview of the DESI Legacy Imaging Surveys. AJ 157, 168 (2019). 696
- 697 Duncan, K. J. All-purpose, all-sky photometric redshifts for the Legacy Imaging Surveys Data Release 8. MNRAS 512, 3662-19. 698 3683 (2022).
- Oke, J. B. et al. The Keck Low-Resolution Imaging Spectrometer. PASP 107, 375 (1995). 20
- McCarthy, J. K. et al. Blue channel of the Keck low-resolution imaging spectrometer in Optical Astronomical Instrumen-21.tation (ed D'Odorico, S.) 3355 (1998), 81-92. 701
- Steidel, C. C. et al. A Survey of Star-forming Galaxies in the $1.4 \lesssim z \lesssim 2.5$ Redshift Desert: Overview. ApJ 604, 534–550 702 22703 (2004)
- Rockosi, C. et al. The low-resolution imaging spectrograph red channel CCD upgrade: fully depleted, high-resistivity CCDs 704 23 for Keck in Ground-based and Airborne Instrumentation for Astronomy III (eds McLean, I. S., Ramsay, S. K. & Takami, H.) 7735 (2010), 77350R. 706
- 24.Prochaska, J. et al. PypeIt: The Python Spectroscopic Data Reduction Pipeline. The Journal of Open Source Software 5, 707 2308 (2020). 708
- 25Dawson, K. S. et al. The Baryon Oscillation Spectroscopic Survey of SDSS-III. AJ 145, 10 (2013). 709
- 710 26 Chambers, K. C. et al. The Pan-STARRS1 Surveys. arXiv e-prints, arXiv:1612.05560 (2016).
- Jarrett, T. H. et al. The Spitzer-WISE Survey of the Ecliptic Poles. ApJ 735, 112 (2011). 711 27.
- Lang, D., Hogg, D. W. & Schlegel, D. J. WISE Photometry for 400 Million SDSS Sources. AJ 151, 36 (2016). 28.712
- Gordon, Y. A. et al. A Quick Look at the 3 GHz Radio Sky. I. Source Statistics from the Very Large Array Sky Survey. 29. 713 714 ApJS 255, 30 (2021)
- Helfand, D. J., White, R. L. & Becker, R. H. The Last of FIRST: The Final Catalog and Source Identifications. ApJ 801, 30. 715 716 26 (2015).

- Calistro Rivera, G., Lusso, E., Hennawi, J. F. & Hogg, D. W. AGNfitter: A Bayesian MCMC Approach to Fitting Spectral Energy Distributions of AGNs. ApJ 833, 98 (2016). 717 31. 718
- Hardcastle, M. J. et al. The LOFAR Two-Metre Sky Survey. VI. Optical identifications for the second data release. A&A 32. 719 678, A151 (2023). 720
- 33. Mostert, R. I. J. et al. Constraining the giant radio galaxy population with machine learning and Bayesian inference. arXiv 721 *e-prints*, arXiv:2405.00232 (2024). Oei, M. S. S. L. *et al.* Luminous giants populate the dense Cosmic Web: The radio luminosity-environmental density relation 722
- 723 34.for radio galaxies in action. arXiv e-prints, arXiv:2404.17776 (2024). Wen, Z. L. & Han, J. L. A catalog of 1.58 million clusters of galaxies identified from the DESI Legacy Imaging Surveys. 724
- 35. 725 arXiv e-prints, arXiv:2404.02002 (2024). 726
- 36. Pasini, T. et al. Radio galaxies in galaxy groups: kinematics, scaling relations, and AGN feedback. MNRAS 505, 2628-2637 727 728 (2021)
- Arnaud, M. *et al.* The universal galaxy cluster pressure profile from a representative sample of nearby systems (REXCESS) and the Y_{SZ} M_{500} relation. A&A **517**, A92 (2010). 729 37 730 38. Sun, M. et al. The Pressure Profiles of Hot Gas in Local Galaxy Groups. ApJ 727, L49 (2011).
- 731 Cooke, R. J. & Fumagalli, M. Measurement of the primordial helium abundance from the intergalactic medium. Nature 39. 732 Astronomy 2, 957-961 (2018). 733
- Lovisari, L., Reiprich, T. H. & Schellenberger, G. Scaling properties of a complete X-ray selected galaxy group sample. A&A 734 40. 735 573, A118 (2015).
- Ricciardelli, E., Quilis, V. & Planelles, S. The structure of cosmic voids in a ΛCDM Universe. MNRAS **434**, 1192–1204 (2013). Upton Sanderbeck, P. R., D'Aloisio, A. & McQuinn, M. J. Models of the thermal evolution of the intergalactic medium after 41. 736 42. reionization. MNRAS 460, 1885–1897 (2016). 738
- 739 43. Tuominen, T. et al. An EAGLE view of the missing baryons. A&A 646, A156 (2021).
- 44. Oei, M. S. S. L. et al. Measuring the giant radio galaxy length distribution with the LoTSS. A&A 672, A163 (2023). 740
- Heckman, T. M. & Best, P. N. The Coevolution of Galaxies and Supermassive Black Holes: Insights from Surveys of the Contemporary Universe. ARA&A **52**, 589–660 (2014). 741 45.742
- Correa, C. M. et al. Redshift-space effects in voids and their impact on cosmological tests. Part I: the void size function. 743 46. MNRAS 500, 911-925 (2021). 744
- 745 47. Hardcastle, M. J. & Krause, M. G. H. Numerical modelling of the lobes of radio galaxies in cluster environments. MNRAS 430, 174–196 (2013). 746
- Barrows, R. S., Comerford, J. M., Stern, D. & Assef, R. J. A Catalog of Host Galaxies for WISE-selected AGN: Connecting Host Properties with Nuclear Activity and Identifying Contaminants. ApJ **922**, 179 (2021). Chen, Z.-F., Pan, D.-S., Pang, T.-T. & Huang, Y. A Catalog of Quasar Properties from the Baryon Oscillation Spectroscopic 747 48.748
- 49. 749 Survey. ApJS 234, 16 (2018). 750
- Oei, M. S. S. L. Code Ocean capsule for 'Black hole jets on the scale of the Cosmic Web'. 2024. 751 50.