

¹ Black hole jets on the scale of the Cosmic Web

²² Summary Paragraph

 When sustained for megayears [\[1,](#page-5-0) [2\]](#page-5-1), high-power jets from supermassive black holes become the Uni- verse's largest galaxy-made structures [\[3\]](#page-5-2). By pumping electrons, atomic nuclei, and magnetic fields into the intergalactic medium, these energetic flows affect the distribution of matter and magnetism in the Cosmic Web [\[4–](#page-5-3)[6\]](#page-5-4), and could have a sweeping cosmological influence if they reached far at early epochs. For the last fifty years, the known size range of black hole jet pairs terminated at 4.6– 5.0 Mpc [\[7](#page-5-5)[–9\]](#page-5-6), or 20–30% of a cosmic void radius in the Local Universe [\[10\]](#page-5-7). An observational 29 lack of longer jets, as well as theoretical results [\[11\]](#page-5-8), thus suggested a growth limit at \sim 5 Mpc [\[12\]](#page-5-9). Here we report observations of a radio structure spanning ∼7 Mpc, or ∼66% of a coeval cosmic ³¹ void radius, apparently generated by a black hole between $4.4^{+0.2}_{-0.7}$ –6.3 Gyr after the Big Bang. The structure consists of a northern lobe, a northern jet, a core, a southern jet with an inner hotspot, and a southern outer hotspot with a backflow. This system demonstrates that jets can avoid destruc- tion by magnetohydrodynamical instabilities over cosmological distances, even at epochs when the 35 Universe was $7-15\frac{+6}{2}$ times denser than it is today. How jets can retain such long-lived coherence is presently unknown.

³⁷ Keywords: Active galactic nuclei, astrophysical jets, giant radio galaxies, intergalactic medium

³⁸ 1 Main text

³⁹ To quantify the impact of black hole energy transport on the intergalactic medium (IGM), radio images ⁴⁰ from the International LOFAR Telescope (ILT) have recently been searched [e.g. [9,](#page-5-6) [13](#page-5-10)[–15\]](#page-5-11) for Mpc-⁴¹ scale galactic outflows. In particular, our team systematically scanned the ILT's ongoing northern sky

- 42 survey at wavelength $\lambda = 2.08$ m both with machine learning and by eye the latter with significant
- ⁴³ contributions from citizen scientists [\[16\]](#page-5-12). This endeavour has increased the number of known Mpc-scale
- ⁴⁴ outflows from a few hundred to over eleven thousand [\[15\]](#page-5-11). Our largest find is the outflow shown in Fig. [1,](#page-1-0) which we name Porphyrion. The source, of angular length $\phi = 13.4' \pm 0.1'$, appears unusually thin.

Fig. 1: Deep radio images of a 7 Mpc–long, black hole–driven outflow at central wavelengths $\lambda = 2.08$ m and $\lambda = 0.46$ m. These images, (a) and (b), were taken with the ILT and uGMRT, respectively, and have resolutions of 6.2" and 4.3". Panel (a)'s inset shows ILT VLBI imagery at $\lambda =$ 2.08 m and a resolution of 0.4". Panel (b)'s inset shows Legacy DR10 optical–infrared imagery. The larger images cover $15' \times 15'$ of sky, whilst the insets cover $1' \times 1'$. For scale, we show the stellar Milky Way disk (diameter: 50 kpc) and a ten times inflated version.

Fig. 2: In our imagery, only the southern host galaxy candidate features a radio extension along Porphyrion's overarching jet axis. For the central $3' \times 3'$ sky area, we show a uGMRT image at $\lambda = 0.46$ m and 3.6'' resolution. We detect the southern galaxy's radio extension, directed towards the north-northeast, at 5 s.d. (σ) significance. The contours denote 3σ , 5σ , 10σ , and 100σ .

 To investigate from which galaxy along the jet axis the outflow originates, we processed ILT very-long-⁴⁶ baseline interferometry (VLBI) data of the central $4' \times 4'$. At a spatial resolution of 3 kpc, the image ⁴⁷ (Fig. [1'](#page-1-0)s top panel inset and Fig. [2.2\)](#page-9-0) shows lone, unresolved radio sources in two galaxies, in both cases implying active accretion onto a supermassive black hole (SMBH). Because the detection of jets near either black hole (and along the overarching NNE–SSW axis) would clarify Porphyrion's origin, we performed deep follow-up observations with the Upgraded Giant Metrewave Radio Telescope (uGMRT) at $\lambda = 0.46$ m. The resulting image and ancillary DESI Legacy Imaging Surveys (Legacy) optical–infrared ⁵² data (Fig. [1'](#page-1-0)s bottom panel) reveal that the outflow protrudes from a massive $(M_{\star} = 6.7^{+1.4}_{-1.4} \cdot 10^{11} M_{\odot})$ galaxy. This is visually clear in Fig. [2,](#page-2-0) which is processed to highlight the radio morphologies of the two central galaxies. Of these, the southernmost galaxy uniquely displays a 5σ extension along Porphyrion's overarching jet axis. We observed this galaxy with the Low Resolution Imaging Spectrometer (LRIS) on $_{56}$ the W. M. Keck Observatory's Keck I Telescope, measuring a spectroscopic redshift $z = 0.896 \pm 0.001$ $_{57}$ (Fig. [3'](#page-3-0)s top panel). We witness Porphyrion at $t_{\text{BB}} = 6.3$ Gyr after the Big Bang.

⁵⁸ The outflow's angular length and redshift entail a sky-projected length $l_p = 6.43 \pm 0.05$ Mpc. This ⁵⁹ makes Porphyrion the projectively longest known structure generated by an astrophysical body. The ⁶⁰ outflow's total length exceeds this projected length, but by how much depends on the unknown inclination ⁶¹ of the jets with respect to the sky plane. Deprojection formulae [\[14\]](#page-5-13) predict a total length $l = 6.8^{+1.2}_{-0.3}$ Mpc, ⁶² with expectation $\mathbb{E}[L | L_p = l_p] = 7.28 \pm 0.05$ Mpc (Methods). We thus estimate Porphyrion to be ⁶³ ∼7 Mpc long in total. Spanning ∼66% of the radius of a typical cosmic void at its redshift, the outflow ⁶⁴ is truly cosmological. Surprisingly, SMBH jets can remain collimated over several megaparsecs, despite ⁶⁵ the growth of (magneto)hydrodynamical (MHD) instabilities — chiefly Kelvin–Helmholtz instabilities — ⁶⁶ predicted theoretically and seen in simulations of shorter jets [e.g. [11\]](#page-5-8). Similarly, prolonged entrainment 67 of mass from the IGM, even at $z \gtrsim 1$, does not necessarily destabilise jets. No MHD simulations of Mpcss scale jets yet exist: the spatio-temporal grids required imply a numerical cost $\sim 10^2$ times higher than ⁶⁹ that of state-of-the-art runs. Outflows like Porphyrion thus offer a window into a jet physics regime that, ⁷⁰ at present, cannot be explored numerically.

⁷¹ Active galactic nuclei (AGN) with accretion disks extending to the innermost stable circular orbits ⁷² of their SMBHs efficiently convert the gravitational potential energy of infalling matter into radiation, ⁷³ and are thus called radiatively efficient (RE); all others are called radiatively inefficient (RI) [\[17,](#page-5-14) [18\]](#page-5-15).

Fig. 3: Both rest-frame ultraviolet–optical spectroscopy and radio–ultraviolet photometry demonstrate that the outflow's host galaxy harbours an RE AGN. a) LRIS spectrum exhibiting hydrogen, carbon, oxygen, and neon emission. The forbidden lines from multiply ionised oxygen and neon (dark red) could not be generated by even the hottest stars, and instead stem from the narrowline region of an RE AGN at a redshift $z = 0.896 \pm 0.001$. b) Bayesian inference of the galaxy's SED (Methods) favours the presence of an AGN accretion disk (dark blue) with an obscuring torus (purple), again indicating radiative efficiency.

 In RE AGN, the luminous accretion disk photo-ionises a circumnuclear region emitting narrow, and often forbidden, spectral lines. The Keck-observed prominence of forbidden ultraviolet–optical lines from $\frac{76}{10}$ oxygen and neon (chiefly that of the [O III]λ5007 line, which is 10.3 ± 0.2 times brighter than the Hβ line) therefore reveals the presence of an RE AGN [\[19\]](#page-5-16). Bayesian inference of the galaxy's spectral energy distribution (SED; Methods and Fig. [3'](#page-3-0)s bottom panel) independently suggests the presence of a $_{79}$ luminous SMBH accretion disk with an obscuring torus: our model requires these structures to explain the observed infrared (WISE) and near-ultraviolet (Legacy) flux levels, which exceed those possible with cold dust and stars alone.

82 By contrast, all previous record-length outflows, such as 3C 236 $(l_p = 4.6 \text{ Mpc}; [7])$ $(l_p = 4.6 \text{ Mpc}; [7])$ $(l_p = 4.6 \text{ Mpc}; [7])$, J1420–0545 $(l_p = 1.6 \text{ Mpc}; [7])$ 83 4.9 Mpc; [\[8\]](#page-5-17)), and Alcyoneus ($l_p = 5.0$ Mpc; [\[9\]](#page-5-6)), are fuelled by RI AGN in recent history ($t_{\text{BB}} = 10.2-$ 84 12.4 Gyr). Whereas RI AGN occur primarily in evolved, 'red and dead' ellipticals [\[17\]](#page-5-14), RE AGN feature ⁸⁵ vigorous gas inflows and are thus generally found in star-forming galaxies. Indeed, in the first billions 86 of years of cosmic time, RE AGN dominated the radio-luminous AGN population [\[20\]](#page-5-18). The potential 87 of Mpc-scale outflows to spread cosmic rays, heat, heavy atoms, and magnetic fields through the IGM ⁸⁸ is particularly high if large specimina could emerge from the type of AGN abundant at early epochs,

Fig. 4: By superimposing Porphyrion's total length and radio luminosity on evolutionary tracks from dynamical modelling, we inferred the outflow's two-sided jet power and age. We assumed the host galaxy to reside in a galaxy group bordering voids, through which the jets eventually travel. The width and height of Porphyrion's uncertainty ellipse both cover 68% of probability centred around the median (green dot).

89 when the Universe was smaller. The discovery of a 7 Mpc–long, RE AGN–fuelled outflow before cosmic ⁹⁰ half-time therefore highlights the hitherto understudied cosmological transport capabilities of Mpc-scale 91 **outflows.**

92 In the Local Universe, \sim 30% of all luminous Mpc-scale outflows reside in galaxy clusters, \sim 60% in 93 galaxy groups, and the remaining ∼10% in more dilute parts of filaments, in sheets, or in voids [\[21\]](#page-5-19). The 94 Legacy DR10 (shown in Fig. [1'](#page-1-0)s bottom panel inset) suggests that Porphyrion does not originate from a ⁹⁵ galaxy cluster: the closest known cluster [\[22\]](#page-5-20) lies at a comoving distance of 30^{+12}_{-17} Mpc, or 31^{+14}_{-16} cluster ⁹⁶ radii (Methods). The nearest Planck Sunyaev–Zel'dovich detection [\[23\]](#page-5-21) is ∼2° away. Concordantly, studies 97 have found that jet-fuelling RE AGN avoid rich environments [\[24,](#page-5-22) [25\]](#page-5-23). In a sphere with a comoving 98 radius of 10 Mpc centred around Porphyrion's host, we counted 35 ± 6 other Legacy-detected galaxies. ⁹⁹ By also performing galactic neighbour counts for a control sample of galaxies at comparable redshifts, ¹⁰⁰ and by assuming that galactic neighbour counts increase with circumgalactic Cosmic Web density, we 101 estimated Porphyrion's circumgalactic Cosmic Web density percentile to be 42^{+26}_{-23} % (Methods). This ¹⁰² suggests that Porphyrion does not originate from a void. The straightness of the outflow implies a low 103 peculiar speed $(v_p \lesssim 10^2 \text{ km s}^{-1})$, consistent with the host being at the bottom of a local gravitational ¹⁰⁴ potential well. The evidence implies that Porphyrion originates from a Cosmic Web filament, and from ¹⁰⁵ a galaxy group in particular. Vast voids, which make up the bulk (∼80%) of the Universe's volume ¹⁰⁶ [\[26\]](#page-6-0), surround such structures in most directions. Jets as long as Porphyrion's thus encounter void-¹⁰⁷ like densities and temperatures with considerable probability. Indeed, the collimated nature of the jets ¹⁰⁸ favours scenarios in which they descend into voids, as jets gain resilience against Kelvin–Helmholtz ¹⁰⁹ instabilities when the ambient density declines [e.g. [11\]](#page-5-8). Dynamical modelling suggests a two-sided jet 110 power $Q = 1.3 \pm 0.1 \cdot 10^{39}$ W and an age $T = 1.9^{+0.7}_{-0.2}$ Gyr (Fig. [4;](#page-4-0) Methods). The outflow's average 111 expansion speed $v = 0.012$ c, comparable to Alcyoneus' [\[9\]](#page-5-6). In voids and the warm–hot IGM, the speed ¹¹² of sound $c_s \sim 10^{0}$ –10¹ km s⁻¹: the jets grow hypersonically at Mach numbers $\mathcal{M} \sim 10^{2}$ –10³ and drive ¹¹³ strong shocks into voids. Porphyrion's jets have carried an energy $E = QT = 8\frac{+2}{1} \cdot 10^{55}$ J into the IGM $_{114}$ — an amount comparable to the energy released during galaxy cluster mergers [e.g. [27\]](#page-6-1). This suggests ¹¹⁵ that the outflow is among the most energetic post–Big Bang events to have occurred in its Cosmic Web ¹¹⁶ region. Even though the SMBH might have gained a significant fraction of its mass while powering the ¹¹⁷ jets (Δ M_{\bullet} > $2\frac{E}{c^2} = 9\frac{+2}{1}$, 10⁸ M_{\odot}), it appears to have maintained a constant spin axis throughout ¹¹⁸ gigayears of activity. Shocks running perpendicular to the jets dissipate enough heat into the filament 119 to increase its temperature by $\Delta T \sim 10^7$ K and its radius by $\Delta r \sim 1$ Mpc (Methods). Outflows like ¹²⁰ Porphyrion thus locally alter the Cosmic Web's shape.

 Figure [4](#page-4-0) illustrates that the radio luminosities of Mpc-long outflows with constant jet power ini- tially decrease before stabilising to a jet power–dependent level. Active outflows not only lengthen, but also grow volumetrically [\[15\]](#page-5-11); consequently, the mean radio luminosity per unit of lobal volume drops over time. In turn, lobal radio surface brightnesses decrease [\[21\]](#page-5-19), impeding outflow detection [\[14,](#page-5-13) [15\]](#page-5-11). As Fig. [1](#page-1-0) evinces, Porphyrion borders on the noise of leading current-day telescopes; thus, outflows further progressed on the same evolutionary track hitherto evade detection. Similar outflows are likewise unde- tectable at lower jet powers and at higher redshifts, where increased inverse Compton scattering with $_{128}$ the CMB diverts electron energy away from synchrotron radiation — causing lower radio luminosities at fixed jet powers [\[28\]](#page-6-2). Problematically, cosmological surface brightness dimming further reduces radio sur-130 face brightnesses by a factor of $(1+z)^{3-\alpha}$, where α is the radio spectral index. Statistical modelling [\[14,](#page-5-13) [15\]](#page-5-11) indeed suggests that the detectable population is just the tip of the iceberg: owing to their apparent faintness, most Mpc-scale outflows are still concealed by noise. These arguments, and the fact that our search covered only ∼15% of the sky, imply the existence of a hidden population of outflows with sizes comparable to, and possibly larger than, Porphyrion's.

¹³⁵ Porphyrion indicates that RE AGN may be at least as effective at generating Mpc-scale outflows ¹³⁶ as RI AGN are in the Local Universe. If the comoving number density of actively powered Mpc-scale ¹³⁷ outflows has remained roughly constant over time at $\sim 10^1$ (100 Mpc)⁻³ [\[14,](#page-5-13) [15\]](#page-5-11), and a comoving vol-¹³⁸ ume of (100 Mpc)³ contains ∼10² filaments, then there would exist ∼10⁻¹ actively powered Mpc-scale outflows in every filament at every instant. As their jets endure for $\sim 10^{-2}$ – 10^{0} Gyr [\[1,](#page-5-0) [3,](#page-5-2) [9\]](#page-5-6), $\sim 10^{1}$ 139 ¹⁴⁰ Mpc-scale outflows may have been generated in every filament throughout cosmic history. If jet pow- $_{141}$ ers $Q \sim 10^{38}$ W are typical [\[1,](#page-5-0) [9,](#page-5-6) [28\]](#page-6-2), Mpc-scale outflows induce significant heating (ΔT $\sim 10^{6}$ K) Δt ¹⁴² and expansion ($\Delta r \sim 10^{-1}$ Mpc) of cosmic filaments (Methods), which comprise the Universe's primary ¹⁴³ baryon reservoir. Whereas AGN feedback has been known to maintain the thermodynamic state in the $144 \sim 1 \text{ Mpc}^3$ -scale volumes of galaxy clusters, Porphyrion's discovery highlights the importance of black

¹⁴⁵ hole energy transport in the Cosmic Web at large.

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²²² 2 Methods

²²³ Throughout this work, we assume a flat, inflationary ΛCDM cosmological model with parameters from 224 Planck Collaboration et al. [\[1\]](#page-21-0): $h = 0.6766, \Omega_{BM,0} = 0.0490, \Omega_{M,0} = 0.3111, \text{ and } \Omega_{\Lambda,0} = 0.6889.$ We 225 define $\Omega_{\text{DM},0}$ = $\Omega_{\text{M},0}$ – $\Omega_{\text{BM},0}$ = 0.2621 and $H_0 \coloneqq h \cdot 100 \text{ km s}^{-1} \text{ Mpc}^{-1}$. Furthermore, we define the spectral index α so that it relates to flux density F_{ν} at frequency ν as $F_{\nu} \propto \nu^{\alpha}$. Under this convention, ²²⁷ synchrotron spectral indices are *positive* (i.e. $\alpha = \frac{5}{2}$) for the lowest frequencies and *negative* for higher ²²⁸ frequencies. As the restoring PSFs may not be perfectly circular, all reported resolutions are effective resolutions. In other works, Mpc-scale outflows are usually called 'giant radio galaxies'.^{[1](#page-7-0)} 229

²³⁰ ILT observations and data reduction

 The International LOFAR Telescope [ILT; [3\]](#page-21-1) is exquisitely sensitive to the metre-wavelength synchrotron radiation generated by electrons and positrons in the first tens to hundreds of megayears after their acceleration to relativistic energies. Consequently, the second data release [DR2; [4\]](#page-21-2) of the LOFAR Two- metre Sky Survey [LoTSS; [5\]](#page-21-3), the ILT's ongoing northern sky survey in the 120–168 MHz frequency band, has revealed millions of galaxies boasting supermassive black hole (SMBH) jets.

[2](#page-7-1)36 After discovering Porphyrion², the outflow presented in this work, we extracted a total of 16 hours of $_{237}$ DDFacet-calibrated visibilities [\[6\]](#page-21-4) from LoTSS pointings P228+60 and P233+60 (Project ID: LT5.007). $_{238}$ Following van Weeren *et al.* [\[7\]](#page-21-5), we subtracted all sources far away from the target, performed phase ²³⁹ shifting and averaging, and self-calibrated the resulting data. This removed residual ionospheric artefacts around ILTJ153004.28+602423.2, the brightest source in the arcminute-scale vicinity of the northern ²⁴¹ lobe. We subsequently performed joint deconvolution on the recalibrated target visibilities with WSClean $_{242}$ [\[8\]](#page-21-6) using Briggs weighting -0.5 , yielding the 6.2"-resolution image of Fig. [1'](#page-1-0)s top panel. The noise level is ²⁴³ $\sigma = 25$ Jy deg⁻² at its lowest. The outflow appears thin: its width is nowhere more than a few percent of ²⁴⁴ its length. We defined Porphyrion's angular length as the largest possible great-circle distance between a ²⁴⁵ point in the southern hotspot and a point in the northern lobe. The arc connecting these points defines ²⁴⁶ the overarching jet axis, and we measured its position angle to be $27 \pm 1^{\circ}$.

 To investigate the presence of diffuse structure, we applied Gaussian tapering to the weights of the ²⁴⁸ recalibrated target visibilities. The taper's FWHM in the (u, v) -plane was chosen such that the FWHM of the corresponding Gaussian in the sky plane equals 15′′ ²⁴⁹ . Again performing deconvolution with WSClean $_{250}$ using Briggs weighting -0.5 (albeit in multi-scale mode this time), we obtained the 19.8"-resolution ²⁵¹ image of Fig. [2.1.](#page-8-0) This image reveals the northern lobe more clearly. The noise level is $\sigma = 4.8$ Jy deg⁻². To obtain a high-resolution image of Porphyrion, we reprocessed the P233+60 data, including LOFAR's international stations, from scratch using the LOFAR-VLBI pipeline [\[9\]](#page-21-7). This pipeline builds upon the calibration pipeline for the Dutch part of the array to calibrate the international stations. We derived the dispersive phase corrections and gain corrections for the international stations by calibrat- ing against a bright and compact radio source near the target. In this case, we used the aforementioned ILTJ153004.28+602423.2, a known source from the Long-Baseline Calibrator Survey [LBCS; [10,](#page-21-8) [11\]](#page-21-9). To reduce interference from unrelated radio sources in Porphyrion's angular vicinity, we phased up LOFAR's core stations to narrow down the field of view and only considered data from long baselines to calcu- late the calibration solutions. With the calibration solutions applied in the direction of the target, we $_{261}$ again performed deconvolution with WSClean (but using Briggs weighting 0) to obtain a 0.4"-resolution image, which we show partially in Fig. [1'](#page-1-0)s top panel inset and fully in Fig. [2.2.](#page-9-0) The noise level is ²⁶³ $\sigma = 2.7 \cdot 10^3$ Jy deg⁻² at its lowest. This image, which covers the central one-third of the total jet system, $_{264}$ reveals synchrotron emission at 42σ significance from active galactic nuclei (AGN) in only two galaxies, 19′′ ²⁶⁵ apart. Both lie along the outflow's jet axis nearly halfway between its endpoints. We considered $_{266}$ these galaxies, J152933.03+601552.5 and J152932.16+601534.4, to be Porphyrion's host candidates. In contrast to other radio-emitting structures along Porphyrion's axis, such as the southern complex inter- preted as an inner hotspot, these candidates have optical counterparts in Legacy Surveys DR10 imagery (see Fig. [1'](#page-1-0)s bottom panel inset).

¹Although Mpc-scale outflows are generated by galaxies, they are not galaxies themselves; therefore, referring to them as a class of 'galaxies' could cause confusion. In addition, Mpc-scale outflows may have been primarily studied through radio observations, but their synchrotron losses (like their other radiative losses) appear to have only a minor effect on their evolution [\[2\]](#page-21-10), suggesting that 'radio' should not be used in a name meant to describe these objects intrinsically. Finally, while 'giant' appears apt, it is also vague; we thus prefer 'Mpc-scale'.

² Porphyrion was the son of Ouranos, the Greek primordial sky deity. According to Ps.-Apollodorus, he and Alcyoneus were the greatest of the Gigantes (Giants), while Pindar called him the 'king of the Giants'. He was str Gigantomachy — the battle between the Giants and the Olympian gods for supremacy over the Cosmos.

Fig. 2.1: ILT image at central wavelength $\lambda = 2.08$ m, with a resolution of 19.8", highlighting diffuse emission in the northern lobe and southern backflow. We show the same sky region and annotations as in Fig. [1.](#page-1-0) The contours denote 3σ , 5σ , and 10σ .

²⁷⁰ uGMRT observations and data reduction

 $_{271}$ On 13 May 2023, we observed the outflow with the Upgraded Giant Metrewave Radio Telescope [uGMRT; $272 \quad 12$] in Band 4 (550–750 MHz) for a total of 10 hours. On 23 September 2023, we extended these observations with another 5 hours. These observations are part of GMRT Observing Cycle 44 and have project $_{274}$ code 44.101. We requested to record both narrow-band (GSB) and wide-band (GWB) data. Adverse ²⁷⁵ ionospheric conditions during the September run prohibited us from improving upon the images produced ²⁷⁶ with the May run data only. In what follows, we therefore exclusively discuss May run data reduction $_{277}$ and results. We performed calibration with Source Peeling and Atmospheric Modeling [SPAM; [13\]](#page-21-12), start-²⁷⁸ ing out with the GSB data. After direction-dependent calibration, we used Python Blob Detection and 279 Source Finder [PyBDSF; [14\]](#page-21-13) to derive a sky model from the final GSB image, which subsequently served ²⁸⁰ to initialise the direction-dependent calibration of the GWB data. As SPAM was designed with narrow-²⁸¹ band data in mind, following standard practice, we first split the GWB data along the frequency axis, ²⁸² yielding four subbands of 50 MHz width each. We then calibrated each subband independently. A joint ²⁸³ image of four calibrated subbands revealed residual ionospheric artefacts from ILTJ153004.28+602423.2, ²⁸⁴ the same bright source in the vicinity of the northern lobe mentioned earlier. To mitigate these arte-²⁸⁵ facts, we subtracted (on a subband basis) all sources outside of a spherical cap with a 9['] radius centred 286 around J2000 right ascension $\varphi = 15h29m32.0s$ and declination $\theta = 60d15m33.0s$. We then jointly reim-²⁸⁷ aged the four source-subtracted subbands with WSClean, using Briggs weighting 0. This resulted in the ²⁸⁸ 4.3″-resolution image of Fig. [1'](#page-1-0)s bottom panel. The noise level is $\sigma = 3$ Jy deg⁻² at its lowest.

²⁸⁹ In the Legacy Survey DR10 optical imagery shown in Fig. [1'](#page-1-0)s bottom panel inset, we identified two ²⁹⁰ faint galaxies in the arcsecond-scale vicinity of the southern host galaxy candidate. Of these, the galaxy at $(\varphi, \theta) = (232.37969^{\circ}, 60.26029^{\circ})$ emits low-frequency radio emission at 6σ significance. At the 4.3'' 291 ²⁹² resolution of our fiducial uGMRT image, this radio emission is only narrowly separable from the host ²⁹³ galaxy candidate's, thus interfering with establishing the radio morphology of the candidate. Trading ²⁹⁴ depth for resolution, we reimaged the uGMRT data with WSClean using Briggs weighting −0.5, yielding 295 a $3.6''$ resolution. Subsequently, to isolate the radio morphology of J152932.16+601534.4, we fit a circular ²⁹⁶ Gaussian fixed at the sky coordinates of its radio-emitting neighbour. Naturally, we set this Gaussian's full width at half maximum to 3.6 ′′ ²⁹⁷ . Upon subtracting the Gaussian, we obtained our final image; Fig. [2](#page-2-0) ²⁹⁸ shows its central region, where the noise level is $\sigma = 6$ Jy deg⁻² at its lowest. Only the southern (and

Fig. 2.2: Our ILT VLBI image of Porphyrion's central $3.84' \times 3.84'$ at $\lambda = 2.08$ m and $0.4''$ resolution covers a third of the total jet system and reveals two radio-luminous AGN, detected at $\sim 40\sigma$ significance. We show the overarching jet axis (translucent white), determined from the northern lobe and southern hotspot (not shown), to scale for a jet radius of 1 kpc. The jet axis appears to pass through J152932.16+601534.4.

²⁹⁹ most radio-luminous^{[3](#page-9-1)}) host galaxy candidate features an extension along the overarching jet axis seen ³⁰⁰ in Fig. [1.](#page-1-0) In our data, this extension — indicative of a pair of relativistically beamed jets — occurs at $301\quad 5\sigma$ significance.

³⁰² We estimated the probability to find a spurious (i.e. unrelated) radio-luminous AGN (RLAGN) with ³⁰³ jets along Porphyrion's overarching axis in the region where the host galaxy could plausibly reside. To find ³⁰⁴ the sky density of RLAGN with discernible jet orientations at arcsecond-scale resolutions, metre-scale 305 – wavelengths, and 10^1 Jy deg⁻²-scale noise levels, we studied the LoTSS DR1–derived RLAGN sample 306 presented in Hardcastle et al. [\[16\]](#page-21-14). This sample, consisting of 23,344 RLAGN, contains 6,850 RLAGN ³⁰⁷ with discernible jet orientations. The latter population's *average* sky density $\bar{n}_s = 4 \cdot 10^{-3}$ arcmin⁻². 308 Approximating the sky density n_s of spurious RLAGN with discernible jet orientations near Porphyrion's 309 host with \bar{n}_s would be appropriate only if such RLAGN would not cluster in the sky. More optimally, 310 we estimated n_s by first counting, for each such RLAGN (that appears sufficiently far from the edges of the survey footprint), the number of neighbours in disks of radius 1′ ³¹¹ . Next, we divided each count by the solid angle of the disks, and finally determined the sample mean: $n_s = 8 \cdot 10^{-3}$ arcmin⁻².^{[4](#page-9-2)} We estimated ³¹³ the solid angle of the 'strip' in which an unrelated source could be mistaken for Porphyrion's host to be $\Omega_s = 10^0 \times 10^{-1}$ arcmin².^{[5](#page-9-3)} Defining jets 'aligned' with Porphyrion's when their position angle falls within a $_{315}$ range of width $10¹$ deg centred around Porphyrion's position angle, the probability of randomly attaining alignment $p_s = \frac{10^{\circ}}{180^{\circ}} = 6 \cdot 10^{-2}$. One thus expects to encounter $\mathbb{E}[N_s] = n_s \cdot \Omega_s \cdot p_s = 4 \cdot 10^{-5}$ unrelated 317 RLAGN with resolved and aligned jets near Porphyrion's host. Assuming that N_s is Poisson-distributed, 318 one or more such spurious sources appear with a probability $\mathbb{P}(N_s \geq 1) = 1 - e^{-\mathbb{E}[N_s]} \approx \mathbb{E}[N_s]$.^{[6](#page-9-4)} We thus $\lim_{n \to \infty}$ find $\mathbb{P}(N_{\rm s} \geq 1) = 4 \cdot 10^{-5}$; the probability to find a spurious unresolved RLAGN in the same region is $320 \quad 4 \cdot 10^1$ times larger. We conclude that J152932.16+601534.4 is Porphyrion's host galaxy.

³Radio luminosity L_{ν} is, at fixed redshift and large-scale halo mass, approximately proportional to jet power Q [\[2\]](#page-21-10). Under the Blandford–Znajek mechanism [\[15\]](#page-21-15), $Q \propto M_{\bullet}^{2}$ (at fixed magnetic field strength and s generation of Porphyrion's jets entails a significant SMBH mass gain $\Delta M_{\bullet} \sim 10^8 - 10^9$ M_☉, the SMBH must now be massive; hence, a high radio luminosity is expected.

For disks of larger radii, n_s approaches \bar{n}_s .

⁵We limited the strip's angular length by asserting that plausible host candidates lie between Porphyrion's two detected patches of jet emission.
⁶This approximation improves as $\mathbb{E}[N_s]$ decreases.

Fig. 2.3: Ultraviolet–optical rest-frame spectrum of J152933.03+601552.5, the quasarhosting galaxy 19′′ north-northeast of J152932.16+601534.4, Porphyrion's host galaxy. We identify redshifted hydrogen, carbon, oxygen, neon, and magnesium lines, jointly implying $z_s =$ 0.799 ± 0.001 . Forbidden lines from the quasar's narrow-line region are shown in red. The spectrum has been measured with the LRIS on the W. M. Keck Observatory's Keck I Telescope.

³²¹ Keck I observations and data reduction

³²² The literature offers only photometric redshift estimates of the host galaxy. The SDSS DR12 [\[17\]](#page-21-16) reports $z_{\rm p} = 0.68 \pm 0.06$, the Legacy Surveys DR9 [\[18\]](#page-21-17) reports $z_{\rm p} = 0.93 \pm 0.08$, and Duncan [\[19\]](#page-21-18) reports $z_{\rm p} = 0.92 \pm 0.08$. For radio-emitting galaxies like J152932.16+601534.4, we consider the latter estimate ³²⁵ to be most reliable.

 To establish the redshift of Porphyrion's host galaxy with certainty, we measured its (rest-frame) ultraviolet–optical spectrum with the Low Resolution Imaging Spectrometer [LRIS; [20](#page-21-19)[–23\]](#page-21-20) on the W.M. Keck Observatory's Keck I Telescope. Adequate slit placement requires accurate knowledge of the galaxy's coordinates. From the Legacy Surveys DR10 best-fit model, we found that J152932.16+601534.4's centre 330 lies at $(\varphi, \theta) = (232.38410^{\circ}, 60.25960^{\circ})$. The galaxy's half-light radius is 10.1 ± 0.3 kpc. On 23 June 2023, we observed the galaxy for a total of 900 seconds. We used the 600/4000 grism on LRIS' blue side, with 1×2 binning (spatial and spectral, respectively), and the 400/8500 grating on the red side, again with 1×2 binning. During the observations, the seeing was approximately $0.8''$; as we used a $1.5''$ 333 slit, minimal slit losses occurred. Using a slit position angle of -70° , we could simultaneously obtain a spectrum for J152933.03+601552.5, the quasar-hosting galaxy which we initially considered (and then discarded) as a host candidate. We reduced the data with PypeIt [\[24\]](#page-21-21), a Python-based pipeline with features tailored to reducing LRIS long-slit spectroscopy. We flat-fielded and sky-subtracted the data using standard techniques. We used internal arc lamps for wavelength calibration and a standard star for overall flux calibration.

³⁴⁰ The final LRIS-derived spectra of J152932.16+601534.4 and J152933.03+601552.5 are shown in $_{341}$ $_{341}$ $_{341}$ Figs. 3 and [2.3,](#page-10-0) respectively. The corresponding spectroscopic redshifts are $z_s = 0.896 \pm 0.001$ and $z_{s} = 0.799 \pm 0.001$. The uncertainties reflect LRIS' limited spectral resolution as well as systematic ³⁴³ errors in wavelength calibration. The latter spectroscopic redshift can be compared to the value derived ³⁴⁴ for J152933.03+601552.5 by the SDSS BOSS [\[25\]](#page-21-22) on 5 July 2013. Visual inspection of the SDSS BOSS s⁴⁴⁵ spectrum and its best fit indicates a robust spectroscopic redshift $z_s = 0.79836 \pm 5 \cdot 10^{-5}$. The two ³⁴⁶ measurements are in agreement.

³⁴⁷ Spectral energy distribution

³⁴⁸ To further assess the accretion mode of Porphyrion's AGN, and to estimate its host's stellar mass and 349 possibly star formation rate (SFR), we performed spectral energy distribution (SED) inference. Through ³⁵⁰ VizieR, the Astro Data Lab, and the NASA/IPAC Extragalactic Database, we collected catalogued total

³⁵¹ (rather than fixed-aperture) flux densities, relative flux densities, magnitudes, Galactic transmission

- ³⁵² fractions, and total extinctions from rest-frame ultraviolet to radio wavelengths. Figure [2.4](#page-11-0) shows the
- ³⁵³ crossmatching results. It demonstrates that Porphyrion's host galaxy (as identified in Legacy DR10) is,

Fig. 2.4: All flux densities used in the inference of Porphyrion's host galaxy SED occur within an arcsecond of the Legacy DR10–identified host position. Coloured disks show astrometric uncertainties, while grey circles denote angular distances from the Legacy DR10–identified host position. The golden stars mark all other Legacy DR10–identified sources in the angular vicinity of Porphyrion's host.

in view of the astrometric accuracies of the collected catalogue data, the only plausible match. Just 4.3["] 354 northeast from Porphyrion's host galaxy lies another source, which could be either a Milky Way star or a galaxy. Mindful of the possibility of spuriously high flux density measurements as a result of target– neighbour blending, we assessed all images underlying the catalogued estimates by eye. The neighbouring source only appears to be a point of attention for flux density measurements at small wavelengths, 359 such as in the Legacy g- and r-band, where it has flux densities ~100% and ~60% those of the target, $\frac{360}{200}$ respectively. At the Legacy z-band's larger wavelengths, the neighbour's flux density is small (∼20%) relative to the target's. The error induced by blending, which will add only a fraction of the neighbour's flux density, should thus be negligible. Accordingly, the Pan-STARRS and WISE measurements at even larger wavelengths are not compromised by this neighbour.

³⁶⁴ We converted the Legacy relative flux densities to flux densities by multiplying with the reference ³⁶⁵ flux density $F_{\nu} = 3631$ Jy. We converted the Pan-STARRS AB magnitudes to flux densities using the 366 standard relation (e.g. Eq. 1 of Chambers *et al.* [\[26\]](#page-21-23)). We converted the WISE relative flux densities 367 to flux densities by multiplying with the reference flux densities of Jarrett *et al.* [\[27\]](#page-21-24)'s Table [1](#page-12-0). Table 1 368 provides all retained flux densities F_{ν} and the central wavelengths λ they correspond to.

369 Porphyrion's host galaxy lies at a Galactic latitude $b = 47.43194$ °. Fortunately, at these latitudes, ³⁷⁰ the Galactic transmission is high for all bands included in our SED inference. We tabulate estimated 371 transmitted fractions f_t in Table [1.](#page-12-0) For Pan-STARRS i and y , we calculated f_t from total extinctions ³⁷² $A_{\lambda} = 0.022$ and $A_{\lambda} = 0.014$, respectively, via $f_t = 10^{-\frac{2}{5}A_{\lambda}}$. For Legacy g, where Galactic transmission ³⁷³ is lowest, application of the correction factor f_t^{-1} results in a flux density increase of just ∼4%. For all 374 bands, the correction is smaller than the flux density uncertainty. We conclude that, for our purposes, ³⁷⁵ Galactic extinction can be neglected.

 376 Next, using AGNfitter [\[31,](#page-22-0) Martínez-Ramírez et al. in prep.], we determined the SED posterior shown in the bottom panel of Fig. [3.](#page-3-0) The posterior indicates the presence of a luminous SMBH accretion disk ³⁷⁸ with an obscuring torus, confirming the radiatively efficient nature of Porphyrion's AGN. The SED ³⁷⁹ posterior further implies that the stellar mass of Porphyrion's host is $M_{\star} = 6.7 \pm 1.4 \cdot 10^{11} M_{\odot}$. To

Table 1: Flux densities F_{ν} of Porphyrion's host galaxy throughout the electromagnetic spectrum. These are as measured, and thus have not been corrected for Galactic extinction; to do so, we provide Galactic transmission fractions f_t . Entries are sorted by the central wavelengths λ of the observing bands.¹

Band	λ (μ m)	F_{ν} (Jy)	$f_{\rm t}$ (%)
Legacy g	$4.8 \cdot 10^{-1}$	$2.6 \pm 0.2 \cdot 10^{-6}$	96.3
Legacy r	$6.3 \cdot 10^{-1}$	$8.4 \pm 0.4 \cdot 10^{-6}$	97.5
Legacy z	$9.1 \cdot 10^{-1}$	$4.31 \pm 0.08 \cdot 10^{-5}$	98.6
Pan-STARRS i	$7.5 \cdot 10^{-1}$	$1.1 \pm 0.1 \cdot 10^{-5}$	98.0
Pan-STARRS y	$9.6 \cdot 10^{-1}$	$3.3 \pm 0.3 \cdot 10^{-5}$	98.7
WISE W1	$3.4 \cdot 10^{0}$	$2.41 \pm 0.02 \cdot 10^{-4}$	99.8
WISE W2	$4.6 \cdot 10^{0}$	$2.53 \pm 0.05 \cdot 10^{-4}$	99.9
WISE W3	$1.2 \cdot 10^{1}$	$8.1 \pm 0.5 \cdot 10^{-4}$	100
WISE W4	$2.2 \cdot 10^{1}$	$3.6 \pm 0.4 \cdot 10^{-3}$	100
VLASS	$1.0 \cdot 10^5$	$1.4 \pm 0.2 \cdot 10^{-3}$	100
FIRST	$2.1 \cdot 10^5$	$1.6 \pm 0.1 \cdot 10^{-3}$	100
uGMRT Band 4	$4.6 \cdot 10^5$	$2.1 \pm 0.1 \cdot 10^{-3}$	100
LoTSS	$2.1 \cdot 10^6$	$2.4 \pm 0.2 \cdot 10^{-3}$	100

¹ When multiple flux densities or magnitudes from the same band were available in literature catalogues, we picked the highest signal-to-noise ratio measurement. Legacy data come from Dey *et al.* [\[18\]](#page-21-17), Pan-STARRS data from Chambers *et al.* [\[26\]](#page-21-23), WISE
data from Lang *et al.* [\[28\]](#page-21-25), VLASS data from Gordon *et al.* [\[29\]](#page-21-26), FIRST data from Helfand *et* present work, and LoTSS data from Shimwell et al. [\[4\]](#page-21-2).

 gauge the sensitivity of stellar mass estimates for this galaxy to methodological variation, we compare our result to the corresponding stellar mass estimate in the LoTSS DR2 value-added catalogue [\[32\]](#page-22-1). This catalogue's authors derive a stellar mass $M_{\star} = 5.5^{+0.7}_{-0.6} \cdot 10^{11} M_{\odot}$ from SED fits to Legacy g, r, z and WISE W1 and W2 flux densities.^{[7](#page-12-1)} The two stellar mass measurements are in agreement. Due to the lack of rest-frame far-infrared photometry, the SFR of Porphyrion's host is virtually unconstrained by the SED posterior.

³⁸⁶ Radio luminosities and spectral indices

³⁸⁷ To determine metre-wavelength radio luminosities and a metre-wavelength spectral index for Porphyrion, $\frac{388}{100}$ we first measured its flux densities in the 6.2" ILT and 4.3" uGMRT images. We assumed flux scale ³⁸⁹ uncertainties of 10% and 5%, respectively.

390 Summing over all structural components, the outflow's total flux density at $\lambda = 2.08$ m is $F_{\nu} =$ 391 63 \pm 6 mJy. Its total radio luminosity at rest-frame wavelength $\lambda_r = 1.10$ m therefore is $L_{\nu} = 1.4 \pm 0.1$. ³⁹² 10^{26} W Hz⁻¹; the core radio luminosity, $L_{\nu} = 5.3 \pm 0.5 \cdot 10^{24}$ W Hz⁻¹, comprises ~4% of the total. The 393 outflow's total flux density at $\lambda = 0.46$ m is $F_{\nu} = 12.0 \pm 0.6$ mJy. Its total radio luminosity at $\lambda_{\rm r} = 0.24$ m therefore is $L_{\nu} = 2.7 \pm 0.1 \cdot 10^{25} \text{ W Hz}^{-1}$; the core radio luminosity, $L_{\nu} = 4.7 \pm 0.2 \cdot 10^{24} \text{ W Hz}^{-1}$, 395 comprises ∼17% of the total. These data imply a metre-wavelength total spectral index $\alpha = -1.09 \pm 0.08$ and a core spectral index $\alpha = -0.09_{-0.07}^{+0.08}$. Through spectral index–based interpolation, we estimated the ³⁹⁷ total radio luminosity at $\lambda_r = 2$ m to be $L_\nu = 2.8 \pm 0.3 \cdot 10^{26}$ W Hz⁻¹. This latter total radio luminosity ³⁹⁸ is an important input for our dynamical modelling.

³⁹⁹ We calculated directionally resolved metre-wavelength spectral indices by combining the ILT and uGMRT images. Before doing so, we convolved the latter image to the former's resolution. In Fig. [2.5,](#page-13-0) we show two regions of interest from the resulting spectral index map, which consequently has a resolution of 6.2 ′′ ⁴⁰² . To highlight the directions in which our spectral index measurements are informative, we blanked all directions in which the thermal noise–induced spectral index uncertainty exceeds 0.3. The top panel of Fig. [2.5](#page-13-0) shows that J152932.16+601534.4, Porphyrion's host galaxy, has a significantly higher spectral index than J152933.03+601552.5, the aforementioned quasar-hosting galaxy. The former spectral index is consistent with zero, indicating that the onset of synchrotron self-absorption (SSA) in Porphyrion's host galaxy occurs at metre wavelengths. By contrast, the onset of SSA in the quasar-hosting galaxy must occur at longer wavelengths, suggesting a lower lepton energy density and weaker magnetic fields in its synchrotron-radiating region. The bottom panel of Fig. [2.5](#page-13-0) shows that Porphyrion's southern tip features much lower spectral indices, with a gradient along the jet axis. This gradient is consistent with 411 a scenario of a hotspot with backflow in which spectral ageing occurs. Whereas $\alpha = -1.0 \pm 0.2$ at the 412 hotspot's southwestern side, the radio spectra gradually steepen to $\alpha = -1.6 \pm 0.2$ at the hotspot's northeastern side. No spectral trend appears present further downstream.

⁷This stellar mass estimate is not based on the spectroscopic redshift we have obtained through LRIS, but utilises a photometrybased redshift posterior with mean and standard deviation $z_p = 0.92 \pm 0.08$ [\[19\]](#page-21-18).

Fig. 2.5: Metre-wavelength spectral indices around Porphyrion's centre and southern tip. The top panel, which covers $3' \times 3'$, reveals synchrotron self-absorption at metre wavelengths in the host galaxy, consistent with the fuelling of powerful jets. The bottom panel, which covers $2' \times 2'$, reveals a hotspot with backflow. We show the mean spectral index α between 0.46–2.08 m, at a resolution of 6.2". From light to dark, the contours denote thermal noise–induced spectral index uncertainties of 0.05, 0.1, 0.2, and 0.3.

⁴¹⁴ We investigated further whether the spectral index discrepancy between J152932.16+601534.4 and J152933.03+601552.5 constitutes evidence that the former galaxy is Porphyrion's host. For each of the $1.1 \cdot 10^4$ Mpc-scale outflows catalogued by Mostert *et al.* [\[33\]](#page-22-2), we determined LoTSS DR2 and VLASS ⁴¹⁷ core flux densities. LoTSS DR2 core flux densities were available for 1, 238 Mpc-scale outflows, whilst VLASS core flux densities were available for 6, 882. We found 924 Mpc-scale outflows for which both core flux densities were available and computed the corresponding 144 MHz–3 GHz spectral indices. The results are summarised in Fig. [2.6.](#page-14-0) It is likely that some VLASS-detected cores remain undetected in LoTSS DR2, in particular if they have flat or 'inverted' spectra. The result is a bias in Fig. [2.6](#page-14-0) towards

Fig. 2.6: LoTSS–VLASS spectral index distribution of the cores of 924 Mpc-scale outflows. In grey, we indicate the bins in which the core spectral indices of J152932.16+601534.4, Porphyrion's claimed host galaxy, and J152933.03+601552.5 fall. The distribution suggests that the core spectral index of J152932.16+601534.4 is more typical for Mpc-scale outflows than the core spectral index of J152933.03+601552.5. For J152933.03+601552.5, due to a VLASS non-detection, we show the LoTSS– uGMRT Band 4 spectral index.

 lower spectral indices. In addition, by requiring that the LoTSS DR2–detected core is an isolated source on the sky, the core spectral indices of Fanaroff–Riley I–like outflows have likely been selected out. As Porphyrion is a Fanaroff–Riley II outflow, this deselection of Fanaroff–Riley I outflows makes the distribu- tion arguably more representative. The spectral indices in this sample do not show an obvious trend with ₄₂₆ redshift. From Fig. [2.6,](#page-14-0) we conclude that the known core spectral indices of Mpc-scale outflows favour J152932.16+601534.4 over J152933.03+601552.5 as Porphyrion's host, strengthening our identification.

⁴²⁸ Cosmic Web environment

⁴²⁹ Cosmic Web environment characterisations of luminous $(L_{\nu}(\nu = 150 \text{ MHz}) \ge 10^{24} \text{ W Hz}^{-1})$ Mpc-scale 430 outflows in the Local Universe $(z \leq 0.2)$ have recently been obtained [\[34\]](#page-22-3) by localisation in Bayesian $_{431}$ large-scale structure reconstructions and by crossmatching with catalogues of galaxy clusters (M_{500}) ⁴³² 0.6 · 10¹⁴ M_{\odot}) and galaxy groups (M_{500} < 0.6 · 10¹⁴ M_{\odot}). The resulting probability distribution over Cosmic Web environments serves as a prior distribution for Porphyrion's Cosmic Web environment. In the Local Universe, ∼30% of all luminous Mpc-scale outflows reside in clusters, ∼60% in groups, and the remaining ∼10% in more dilute parts of filaments, in sheets, or in voids [\[34\]](#page-22-3). Thus, if this probability distribution does not evolve with redshift and a cluster environment can be excluded, Porphyrion likely originates from a filament. To evaluate whether Porphyrion's host galaxy inhabits a cluster, we extracted ⁴³⁸ right ascensions, declinations, redshifts, and R_{500} -radii from the cluster catalogue of Wen & Han [\[35\]](#page-22-4), 439 which is based on Legacy DR10. Even though these data allow for cluster detections up to $z \sim 1.5$, we did not find a cluster close to Porphyrion's host. To reach this conclusion statistically, we first estimated ⁴⁴¹ cluster redshift uncertainties using $\sigma_z(z) = 0.02 \cdot \frac{z}{0.9} \cdot (1+z)$ for photometric cluster redshifts, as suggested ⁴⁴² by the bottom-right panel of Fig. 7 of Wen & Han [\[35\]](#page-22-4), and $\sigma_z = 0.001$ for spectroscopic cluster redshifts. We neglected uncertainties in cluster right ascensions and declinations. We then Monte Carlo–simulated a redshift for both Porphyrion's host and all clusters (assuming Gaussian redshift distributions), converted right ascensions, declinations, and redshifts into comoving coordinates, and finally identified the cluster nearest to Porphyrion's host. We recorded the comoving distance to this cluster as well as the ratio between the corresponding proper distance and the cluster's R_{500} -radius. We repeated this Monte Carlo procedure millions of times, until the probability distributions over these distance measures converged. The results are shown in Fig. [2.7.](#page-15-0) Around Porphyrion's redshift, the Wen & Han [\[35\]](#page-22-4) photometric cluster ϵ_{450} redshift uncertainties $\sigma_z \approx 0.04$, large enough to force us to consider several clusters as candidates for being the nearest. Each peak corresponds to the smallest possible distance to a possibly nearest cluster. The peak location is determined by both the angle between Porphyrion's host and the cluster and by Porphyrion's redshift. In Monte Carlo realisations such that the cluster redshift matches Porphyrion's, ⁴⁵⁴ the distance is minimal. The nearest cluster lies at a comoving distance of 30^{+12}_{-17} Mpc, or 31^{+14}_{-16} cluster

Fig. 2.7: DESI Legacy Imaging Surveys DR10 galaxy cluster redshift uncertainties induce multimodal, asymmetric probability distributions over measures of distance between Porphyrion's host galaxy and the nearest galaxy cluster. We mark median-centred intervals containing 68% and 95% of all probability. The data suggest that Porphyrion does not originate from a cluster.

⁴⁵⁵ radii (68% probability intervals); the nearest cluster lies at a comoving distance of 30^{+14}_{-22} Mpc, or 31^{+19}_{-23} cluster radii (95% probability intervals). In just 0.1% of all realisations, Porphyrion's host is five or fewer R_{500} -radii away from the nearest cluster.

 To investigate whether a filament or a void environment is more probable, we performed probabilistic galaxy counts using the Legacy data underlying the Wen & Han [\[35\]](#page-22-4) cluster catalogue. We extracted right ascensions, declinations, redshift posterior means, and redshift posterior standard deviations of all Legacy-detected galaxies that lie within 1.5° of Porphyrion's host. In a similar spirit as before, we then Monte Carlo–simulated redshifts (where, for simplicity, we approximated the galaxies' redshift posterior distributions with Gaussian distributions), converted right ascensions, declinations, and redshifts into comoving coordinates, and counted the number of Legacy-detected galaxies (excluding Porphyrion's host) within a sphere of given radius centred around Porphyrion's host. To properly take into account galactic redshift uncertainties, we repeated this Monte Carlo procedure 1, 000 times. In a sphere with a comoving radius of 10 Mpc centred around Porphyrion's host, we counted 35 ± 6 other Legacy-detected galaxies. We then performed analogous probabilistic galactic neighbour counts for a control sample of galaxies at comparable redshifts. We selected controls by demanding that their redshift means do not deviate more than 0.05 from Porphyrion's. To ensure that these mean redshifts are reliable, we further demanded that the redshift standard deviations of controls are less than 0.1. From the available candidate controls, we picked 100 controls at random, and performed the counts for them. Porphyrion's galactic $\frac{473}{2}$ neighbour count, relative to those of the control sample, occurs at percentile $42^{+26}_{-23}\%$. If we assume

⁴⁷⁴ that circumgalactic Cosmic Web density is a monotonic function of the number of galactic neighbours,

Porphyrion's circumgalactic Cosmic Web density percentile will be $42^{+26}_{-23}\%$, too. This suggests that

⁴⁷⁶ Porphyrion does not originate from a void. In line with the expectation for luminous Mpc-scale outflows 477 in the Local Universe, we conclude that Porphyrion most likely originates from a filament.

⁴⁷⁸ Dynamical modelling: jet power and age

⁴⁷⁹ We derived Porphyrion's jet power and age from its length, radio luminosity, cosmological redshift, ⁴⁸⁰ and likely environment by fitting evolutionary tracks. We generated these evolutionary tracks with the ⁴⁸¹ simulation-based analytic outflow model of Hardcastle [\[2\]](#page-21-10). This model requires assumptions on the large-⁴⁸² scale environment in which the dynamics take place. Following the previous section, we suppose that ⁴⁸³ the host galaxy resides in the centre of a galaxy group of mass $M_{500} = 10^{13} M_{\odot}$ (which comprises ⁴⁸⁴ contributions from both dark and baryonic matter) [\[34,](#page-22-3) [36\]](#page-22-5). We assigned the group a universal pressure ⁴⁸⁵ profile [UPP; [37\]](#page-22-6) $p_g(r)$,^{[8](#page-16-0)} which can be parametrised just by M_{500} . To obtain the group's baryon density 486 profile from its pressure profile, we invoked the ideal gas law: $\rho_{g}(r) = \frac{p_{g}(r)(m)}{k_{B}T_{g}}$, where $\langle m \rangle$ is the average ⁴⁸⁷ plasma particle mass and T_g the group temperature. We assumed a pure ¹H–⁴He plasma with a ⁴He ⁴⁸⁸ mass fraction $Y = 25\%$ [e.g. [39\]](#page-22-7), so that $\langle m \rangle \approx \frac{4}{8-5Y} m_{\rm p} = 0.6$ $m_{\rm p}$, where $m_{\rm p}$ is the proton mass. 489 We estimated T_g , which we assumed constant in space and time, using the mass–temperature relation 490 specified by Eq. 9 and Tables 3 and 4 of Lovisari et al. $[40]$:

$$
\frac{k_{\rm B}T_{\rm g}}{2 \text{ keV}} = 0.77 \cdot \left(\frac{M_{500}}{5 \cdot 10^{13} \ h_{70}^{-1} \ M_{\odot}}\right)^{0.61}.
$$
\n(1)

⁴⁹¹ The aforementioned mass implies $T_g = 7 \cdot 10^6$ K. As Mpc-scale outflows reach beyond the edges of ⁴⁹² groups, it was also necessary to estimate the pressure and baryon density in the AGN's more distant ⁴⁹³ surroundings. Following the bottom-right panel of Ricciardelli *et al.* [\[41\]](#page-22-9)'s Fig. 6, we set the baryon overdensity within voids at Porphyrion's redshift to $\delta = -0.7$.^{[9](#page-16-1)} We obtained a void baryon density ⁴⁹⁵ $\rho_v = \rho_{c,0} \Omega_{BM,0} (1+z)^3 (1+\delta) = 9 \cdot 10^{-31} \text{ g cm}^{-3}$, where $\rho_{c,0}$ is today's critical density. Following Upton 496 Sanderbeck et al. [\[42\]](#page-22-10)'s detailed study of IGM temperatures through cosmic time, which suggests a void ⁴⁹⁷ temperature $T_v \sim 10^3$ –10⁴ K at Porphyrion's redshift, we set $T_v = 1 \cdot 10^4$ K. This choice reflects the $\frac{498}{498}$ fact that we are interested in void temperatures near the galaxy group. Again applying the ideal gas ℓ_{499} law, and taking $\langle m \rangle$ as before, we obtained a void pressure $p_v = 1 \cdot 10^{-19}$ Pa. Finally, we defined the 500 external pressure $p_e(r) = p_g(r) + p_v$, baryon density $\rho_e(r) = \rho_g(r) + \rho_v$, and baryon density-weighted ₅₀₁ temperature $T_e(r) = \frac{\rho_g(r) T_g + \rho_v T_v}{\rho_e(r)}$. Figure [2.8](#page-17-0) shows these profiles.

 We explored whether the addition of a filament component would significantly change Fig. [2.8'](#page-17-0)s pro- $_{503}$ files. We assumed a baryon overdensity $\delta = 10$ at the filament spine, and baryon density and temperature $_{504}$ profiles following Tuominen *et al.* [\[43\]](#page-22-11)'s results for massive filaments in the EAGLE simulation. We found pressure and baryon density contributions of an importance similar to or lesser than that of the group, even at Mpc-scale distances. We thus considered the addition of the filament unnecessary, especially in light of model uncertainties such as the group's mass and the surmised validity of extrapolating the group's UPP to Mpc-scale distances.

⁵⁰⁹ We generated 21 evolutionary tracks of 200 time steps each, spanning a range jet powers $Q = 10^{38.8}$ $10^{39.2}$ W. Propagating total length and radio luminosity uncertainties, we obtained $Q = 1.3 \pm 0.1 \cdot 10^{39}$ W $_{511}$ and $T = 1.9^{+0.7}_{-0.2}$ Gyr. The outflow's jet power uncertainty is set by radio luminosity uncertainty while ⁵¹² its age uncertainty is set by total length uncertainty. The inferred Gyr-scale age suggests that treating ⁵¹³ outflow evolution as a process at a single redshift — as is currently done in the model of Hardcastle [\[2\]](#page-21-10) ⁵¹⁴ — is crude for the largest outflows, and may need revision. Each jet's average speed $\langle \beta \rangle := \frac{\langle v \rangle}{c^c} = \frac{l}{c^2 c^T} =$ ⁵¹⁵ 0.58^{+0.04}%, where c is the speed of light. The energy transported by the jets $E = QT = 7.6^{+2.1}_{-0.7}$. 10⁵⁵ J. As ⁵¹⁶ a black hole can redirect at most half of the rest energy of infalling matter to electromagnetic radiation ⁵¹⁷ and jet fuelling, and the energy an RE AGN spends on electromagnetic radiation must at least equal ⁵¹⁸ the energy spent on jet fuelling, the black hole must have gained a mass $\Delta M_{\bullet} > 2\frac{E}{c^2} = 8.5^{+2.4}_{-0.8} \cdot 10^8 M_{\odot}$ ⁵¹⁹ while powering the jets.

⁸Sun *et al.* [\[38\]](#page-22-12) have shown that the UPP applies to galaxy groups, even though the profile has originally been proposed to fit
data on galaxy *clusters* (which have much higher masses: $10^{14} M_{\odot} < M_{500} < 10^{15} M_{\od$

⁽which comprises contributions from both dark and baryonic matter), as Ricciardelli et al. [\[41\]](#page-22-9) considers the latter.

Fig. 2.8: Pressure, baryon density, and temperature external to the outflow, as a function of the proper distance from Porphyrion's AGN, in our dynamical modelling. The profiles consist of contributions from the outflow's presumed galaxy group and the adjacent voids.

⁵²⁰ Total outflow length

⁵²¹ To estimate Porphyrion's total length from its projected length, we perform statistical deprojection. 522 Equation 9 of Oei *et al.* [\[44\]](#page-22-13) stipulates the probability density function (PDF) of an outflow's total length $_{523}$ random variable (RV) L in case its projected length RV L_p is known to equal some value l_p . This PDF 524 is parametrised by the tail index ξ of the Pareto distribution assumed to describe L. We calculate the 525 median and expectation value of L | $L_p = l_p$ for tail indices $\xi = -3$ and $\xi = -4$, the integer values 526 closest to the observationally favoured $\xi = -3.5 \pm 0.5$ [\[44\]](#page-22-13).

⁵²⁷ First, we determine the cumulative distribution function (CDF) of $L | L_p = l_p$ through integration:

$$
F_{L|L_{\rm p}=l_{\rm p}}(l) := \int_{-\infty}^{l} f_{L|L_{\rm p}=l_{\rm p}}(l') \, \mathrm{d}l'
$$
\n
$$
= \frac{-\xi}{2^{1+\xi}\pi} \frac{\Gamma^2\left(-\frac{\xi}{2}\right)}{\Gamma(-\xi)} \int_{1}^{\max\{x,1\}} \frac{x'^{\xi-1}}{\sqrt{x'^2-1}} \, \mathrm{d}x',
$$
\n(2)

 \sum_{528} where $x \coloneqq \frac{l}{l_{\rm p}}$ and $x' \coloneqq \frac{l'}{l_{\rm p}}$. 529 For $\xi = -3$, the CDF concretises to

$$
F_{L|L_{\mathbf{p}}=l_{\mathbf{p}}}(l) = \frac{3}{2} \int_{1}^{\max\{x,1\}} \frac{\mathrm{d}x'}{x'^{4}\sqrt{x'^{2}-1}}
$$

=
$$
\begin{cases} 0 & \text{if } x < 1; \\ \frac{(2x^{2}+1)\sqrt{x^{2}-1}}{2x^{3}} & \text{if } x \ge 1. \end{cases}
$$
 (3)

 $\sum_{i=1}^{530}$ The median conditional total length, l_m , is defined by $F_{L|L_p=l_p}(l_m) \coloneqq \frac{1}{2}$. Numerically, we obtain $x_m \coloneqq$ $\frac{l_m}{l_p} \approx 1.0664$, or $l_m \approx 1.0664$ l_p . As $l_p = 6.43 \pm 0.05$ Mpc, we find $l_m = 6.86 \pm 0.05$ Mpc. An analogous numerical determination of the 16-th and 84-th percentiles then yields $l = 6.9^{+1.6}_{-0.4}$ Mpc.

 533 For $\xi = -4$, the CDF concretises to

$$
F_{L|L_{\rm p}=l_{\rm p}}(l) = \frac{16}{3\pi} \int_{1}^{\max\{x,1\}} \frac{\mathrm{d}x'}{x'^5 \sqrt{x'^2 - 1}} \qquad (4)
$$

$$
= \begin{cases} 0 & \text{if } x < 1; \\ \frac{2}{3\pi} \left(\frac{(3x^2 + 2)\sqrt{x^2 - 1}}{x^4} + 3\arccos\frac{1}{x} \right) & \text{if } x \ge 1. \end{cases}
$$

534 Numerically, we obtain $x_m \approx 1.0515$, or $l_m \approx 1.0515 l_p$, and thus $l_m = 6.76 \pm 0.05$ Mpc. In the same way 535 as before, we find $l = 6.8^{+1.2}_{-0.3}$ Mpc.

 $\mathbb{E}[\text{L} \mid L_p = l_p] (\xi)$. Table 1 of the same ⁵³⁷ work lists $\mathbb{E}[L | L_p = l_p](\xi = -3) = \frac{3\pi}{8}l_p$ and $\mathbb{E}[L | L_p = l_p](\xi = -4) = \frac{32}{9\pi}l_p$. In the case of Porphyrion, 538 these expressions concretise to $\mathbb{E}[L | L_p = l_p](\xi = -3) = 7.58 \pm 0.06$ Mpc and $\mathbb{E}[L | L_p = l_p](\xi = -4) =$ 539 7.28 \pm 0.05 Mpc.

 By conditioning L on more knowledge than a value for L_p alone, statistical deprojection could be made more precise. For example, one could additionally condition on the fact that Porphyrion is generated by a Type 2 radiatively efficient (RE) AGN. If Type 1 RE AGN are seen mostly face-on and Type 2 RE AGN are seen mostly edge-on, as proposed by the unification model [e.g. [45\]](#page-22-14), then the detection of a Type 2 RE AGN would imply that the jets make a small angle with the sky plane. Extending the formulae to include this knowledge is beyond the scope of this work; however, mindful of the associated $_{546}$ deprojection factor–reducing effect, we choose $\xi = -4$ as our fiducial tail index.

⁵⁴⁷ To assess Porphyrion's transport capabilities in a cosmological context, it is instructive to calculate ⁵⁴⁸ its length relative to Cosmic Web length scales. In particular, the outflow's total length relative to the typical cosmic void radius at its epoch is $f_v := l(1+z)R_v^{-1}$, where R_v is the typical comoving cosmic 550 void radius. For $l = 6.8^{+1.2}_{-0.3}$ Mpc, $z = 0.896 \pm 0.001$, and $R_v = 20$ Mpc [\[46\]](#page-22-15), we find $f_v = 64^{+12}_{-2}$ %. For ⁵⁵¹ our fiducial total length $l = 7$ Mpc, we find $f_v = 66\%$.

⁵⁵² Filament shape modification

⁵⁵³ We predict that powerful, long-lived outflows like Porphyrion cause their host galaxies' filaments to $_{554}$ expand thermally. Through lateral shocks, the jets distribute an amount of heat Q_{WHIM} over the warm– ⁵⁵⁵ hot IGM. This medium is sufficiently dilute that plasma interactions can be neglected; as a result, the $_{556}$ ideal gas law, $pV = N k_B T$, may be adopted as the equation of state. Here, p, V, N, and T are the $_{557}$ filament's pressure, volume, plasma particle number, and temperature, respectively; k_B is Boltzmann's ⁵⁵⁸ constant. Assuming a thermodynamic process at constant pressure and particle number, the work W is

$$
W = p\Delta V = Nk_{\rm B}\Delta T. \tag{5}
$$

Before the outflow's emergence, the filament's equation of state is $pV_i = N k_B T_i$, where V_i and T_i are its ⁵⁶⁰ initial volume and temperature, respectively. Upon dividing Eq. [5](#page-19-0) by this equation of state, one obtains

$$
\frac{\Delta V}{V_{\rm i}} = \frac{\Delta T}{T_{\rm i}}.\tag{6}
$$

 $\frac{561}{100}$ Assuming that the filament retains a cylindrical shape, initially with radius r_i and finally with radius r_f , $_{562}$ and using that $\Delta V \coloneqq V_f - V_i$, one obtains

$$
\frac{r_{\rm f}}{r_{\rm i}} = \sqrt{1 + \frac{\Delta T}{T_{\rm i}}}.\tag{7}
$$

563 The radius ratio, $\frac{r_f}{r_i}$, depends only on the ratio between the temperature increase $\Delta T \coloneqq T_f - T_i$ and the ⁵⁶⁴ initial temperature. The temperature increase is

$$
\Delta T = \frac{Q_{\text{WHIM}}}{N C_{\text{p,m}}},\tag{8}
$$

 $_{565}$ where $C_{p,m}$ is the molar heat capacity at constant pressure. For a monatomic gas or a hydrogen plasma, ⁵⁶⁶ $C_{\rm p,m} = \frac{5}{2}R$, where R is the molar gas constant. The number of filamentary electrons and atomic nuclei ⁵⁶⁷ affected by the outflow is

$$
N = \frac{\pi r_{\rm i}^2 L \rho_{\rm i}}{\mu m_{\rm p}},\tag{9}
$$

⁵⁶⁸ where L is the length of the cylindrical segment affected, ρ_i is the initial baryonic mass density, μ is $_{569}$ the average mass of a plasma particle relative to the proton mass, and $m_{\rm p}$ is the proton mass. We ⁵⁷⁰ estimate $\frac{L}{2}$ by multiplying the typical speed of lateral shocks with the outflow's lifetime. We decompose ⁵⁷¹ $\rho_i = \rho_{c,0} \overline{\Omega}_{BM,0} (1+z)^3 (1+\delta)$, where z and δ are the filament's cosmological redshift and baryonic ⁵⁷² overdensity, respectively.

 To estimate Q_{WHIM} given E, the total energy carried by the jets up to the time of observation, we turn to analytical models and numerical simulations. Modelling indicates that just ∼10% of the total energy is lost through radiative processes [\[2\]](#page-21-10). This fraction increases with redshift, as inverse-Compton losses to the CMB become more pronounced. Numerical simulations show that, at least in galaxy clusters, ∼50% of the non-radiated energy is converted into thermal or kinetic energy carried by the shocked medium, and the other ∼50% is converted into thermal or kinetic energy carried by the outflow's lobes [\[47\]](#page-22-16). Over ₅₇₉ time, the kinetic energy turns into thermal energy. It is, at present, unclear how fast remnant lobes mix with the surrounding medium, and how the mixing timescale varies with the latter's density. Here we assume that, at late times, all of the lobes' energy mixes with the surrounding medium. As such, we 582 estimate $Q_{\text{WHIM}} \rightarrow 90\% \cdot E$.

⁵⁸³ We assess the outflow-induced morphological change to Porphyrion's filament by evaluating Eq. [7,](#page-19-1) t_{loss} taking $Q_{\text{WHIM}} = 7 \cdot 10^{55} \text{ J}, r_i \approx r_c = 1.2 \text{ Mpc}$ (a typical filament core radius [\[43\]](#page-22-11)), $L = 2 \cdot 7 \text{ Mpc} = 14 \text{ Mpc}$ ⁵⁸⁵ (assuming that the region beyond the outflow's direct reach that is affected at late times is comparable ⁵⁸⁶ in length to the outflow itself), $z = 0.9$, $1 + \delta = 10$, $\mu = 0.5$, and $T_i = 10^7$ K; we find $\Delta T = 3 \cdot 10^7$ K (an 587 increase of ∼300%) and $r_f = 2.4$ Mpc (an increase of ∼100%). Porphyrion's heat dissipation renders the ⁵⁸⁸ outflow's native filament much hotter and thicker than it would have otherwise been.

⁵⁸⁹ For our cosmological outlook, we assumed a typical jet power and age that are each an order of ⁵⁹⁰ magnitude lower than Porphyrion's. We thus estimated the combined energy carried by 10 Mpc-scale

⁵⁹¹ outflows to be $Q_{\text{WHIM}} = 7 \cdot 10^{54}$ J. Assuming non-overlapping affected regions, we estimated $L =$ $10 \cdot 2 \cdot 1$ Mpc = 20 Mpc. Leaving all other parameters identical, we find $\Delta T = 2 \cdot 10^6$ K (an increase of $_{593}$ ~20%) and $r_f = 1.3$ Mpc (an increase of ~10%).

Quasar mass–based host galaxy candidate elimination

SDSS J152933.03+601552.5 is the quasar-hosting galaxy 19′′ north-northeast of J152932.16+601534.4, the galaxy we have identified as Porphyrion's host. We initially also considered SDSS $_{597}$ J152933.03+601552.5 as a host galaxy candidate. However, aforementioned arguments involving the pres- ence of jets and their orientation and, to a lesser degree, arguments involving core radio luminosity and core synchrotron self-absorption all favour J152932.16+601534.4. We now discuss how our results would change if, instead, SDSS J152933.03+601552.5 were Porphyrion's host galaxy. Doing so will lead to a contradiction that disproves this alternative hypothesis.

 First, we discuss results that do not require dynamical modelling. To start with, Porphyrion would ϵ_{003} remain generated by an RE AGN. The host galaxy redshift would decrease from $z = 0.896 \pm 0.001$ to $z = 0.001$ 604 0.799 \pm 0.001, decreasing Porphyrion's projected length from $l_p = 6.43\pm0.05$ Mpc to $l_p = 6.21\pm0.05$ Mpc. $\delta_{0.05}$ Again using $\xi = -4$, the total length would decrease from $l = 6.8^{+1.2}_{-0.3}$ Mpc to $l = 6.5^{+1.2}_{-0.3}$ Mpc and its 606 conditional expectation from $\mathbb{E}[L \mid L_{p} = l_{p}] = 7.28 \pm 0.05$ Mpc to $\mathbb{E}[L \mid L_{p} = l_{p}] = 7.03 \pm 0.06$ Mpc. ⁶⁰⁷ If orientation distinguishes Type 1 from Type 2 RE AGN, as the unification model supposes, then these statistical deprojection results may underestimate Porphyrion's total length. Porphyrion would remain the projectively longest galaxy-made structure identified so far. The host's stellar mass would $d_{0.00}$ decrease from $M_{\star} = 6.7 \pm 1.4 \cdot 10^{11}$ M_{\odot} to $M_{\star} = 4.0^{+0.3}_{-0.3} \cdot 10^{11}$ M_{\odot} , while the SFR would become ⁶¹¹ $S = 4.9^{+0.3}_{-0.4} \cdot 10^1$ M_{\odot} yr⁻¹ [\[48\]](#page-22-17). Porphyrion's total radio luminosity at rest-frame wavelength $\lambda_r = 2$ m 612 would decrease from $L_{\nu} = 2.8 \pm 0.3 \cdot 10^{26} \text{ W Hz}^{-1}$ to $L_{\nu} = 2.2 \pm 0.2 \cdot 10^{26} \text{ W Hz}^{-1}$.

 δ ₆₁₃ Next, we discuss results that come from dynamical modelling. The jet power would decrease from $Q = 1.3 \pm 0.1 \cdot 10^{39}$ W to $Q = 1.0 \pm 0.1 \cdot 10^{39}$ W, while the age would slightly increase from $T = 1.9^{+0.7}_{-0.2}$ Gyr $_{615}$ to $T = 1.9^{+0.7}_{-0.1}$ Gyr. The transported energy would decrease from $E = 7.6^{+2.1}_{-0.7}_{-0.7}$ J to $E = 6.4^{+1.8}_{-0.6}_{-0.6}$. 10^{55} J, 616 and the minimum black hole mass gain from $\Delta M_{\bullet} > 8.5^{+2.4}_{-0.8} \cdot 10^8$ M_{\odot} to $\Delta M_{\bullet} > 7.2^{+2.0}_{-0.7} \cdot 10^8$ M_{\odot}

 Finally, we arrive at a contradiction, as the quasar's SMBH mass (measured from its SDSS BOSS ⁶¹⁸ spectrum) $M_{\bullet} = 2.5 \pm 0.3 \cdot 10^8$ M_{\odot} [\[49\]](#page-22-18). This mass is lower than the minimum mass gain associated to ₆₁₉ the fuelling of Porphyrion's jets. Thus, assuming that SDSS J152933.03+601552.5 is the outflow's host galaxy leads to a contradiction. This argument reaffirms that J152932.16+601534.4 is Porphyrion's host.

623 Data availability. The LoTSS DR2 is publicly available at [https://lofar-surveys.org/dr2](https://lofar-surveys.org/dr2_release.html)_release.html. The authors will share the particular LOFAR, uGMRT, and Keck I Telescope data used in this work upon request.

626 Code availability. The dynamical model used to interpret the outflow is described by Hardcastle [\[2\]](#page-21-10) and available for download at [https://github.com/mhardcastle/analytic.](https://github.com/mhardcastle/analytic) Analysis and plotting code specific to this work is available [\[50\]](#page-22-19) on Code Ocean: [https://codeocean.com/capsule/3908804/tree.](https://codeocean.com/capsule/3908804/tree)

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⁶⁶⁵ provided comments to improve the text.

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